Exploring Design Alternatives for Replicated RAMP Transactions Using Maude

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Abstract—Developing correct, scalable, and fault-tolerant distributed databases is hard and labor-intensive. The increasing complexity of such systems under modern cloud infrastructures, e.g., geo-replicated multi-partitioned datacenters, further limits the number of design alternatives that can be explored in practice. There is therefore a need for the formal analysis of both their qualitative properties, e.g., data consistency, and their quantitative properties, e.g., latency, at an early design stage.

In this paper we use formal modeling and both standard and statistical model checking techniques to explore the design space of replicated RAMP (Read Atomic Multi-Partition) transactions for geo-replicated databases. Specifically, we develop in Maude formal, executable specifications of three replicated RAMP designs, two by the RAMP developers and one by us, and analyze their data consistency properties. We further transform the Maude models into probabilistic rewrite theories for statistical model checking w.r.t. performance properties. Our results: (i) are consistent with the conjectures made by the RAMP developers; (ii) uncover our promising new design that not only provides all crucial data consistency guarantees but also outperforms the other design alternatives.

I. INTRODUCTION

Designing reliable and high-performance distributed systems is significantly hard and labor-intensive. Modern cloud databases that typically run in a geo-replicated environment for availability, scalability, and fault tolerance, have further increased this complexity. For instance, integrating a replication mechanism with strong consistency like Paxos into a distributed database may impose a high latency cost, while more efficient mechanisms with weaker consistency may be unable to offer strong data consistency guarantees. This provides a challenge that designers must both assure and balance data consistency and performance to arrive at mature designs.

To evaluate and improve a system design the only available option is to touch a large code base. This often requires intensive manual efforts, has a high risk of introducing new bugs, and is not repeatable. In practice, very few designs can be explored in this way. For example, in the case of designing replicated RAMP (Read Atomic Multi-Partition) transactions, all designs were only sketched out but not implemented [4].

Formal methods have been advocated to develop and analyze high-level designs of distributed systems in general and cloud databases in particular. One representative formal ecosystem that has shown promise in meeting the above challenges is Maude [9], a rewriting-logic-based formal framework for executable specification and a high-performance analysis toolkit for object-based distributed systems [6], [15], [16], [24], [29]. In particular, Maude’s LTL model checker and the PVeStA statistical model checker [3] have been used to analyze, often for the first time, both correctness and performance of high-level designs of a wide range of state-of-the-art industrial and academic cloud databases such as Apache Cassandra, Google’s Megastore, RAMP, Walter, and ROLA. Model-based performance predictions using PVeStA have shown good correspondence with implementations-based evaluations under realistic deployments for Cassandra, RAMP, Walter, and ROLA [13], [14], [19], [22].

Our Goal. We anticipate that all correct and high-performance distributed databases must undergo both qualitative and quantitative analyses to obtain desirable data consistency and performance guarantees. Moreover, these analyses should be performed at an early design stage to avoid design errors that may be orders of magnitude more costly to eliminate at the implementation stage. In the spirit of achieving this goal, we present the formal designs and analyses of replicated RAMP transactions.

Status Quo of RAMP. The RAMP transaction system, proposed by Bailis et al. [4], is one of the most promising databases that bridge the gap between efficiency (low latency) and strong consistency (correctness) in a distributed setting (the CAP theorem [7]). RAMP offers a correctness property called “Read Atomicity” (RA) which ensures that a given transaction’s updates are either all visible or not visible at all, to other transactions.

The RAMP paper [4] briefly mentions two designs for data replication, but without any details or formal analysis. Given the importance of data replication in modern cloud databases and of making RAMP a production-capable system in geo-replicated environment, there is therefore a clear need for formally specifying and analyzing replicated RAMP transactions.

Our Contributions. A main contribution in this paper is to develop in Maude formal, executable specifications of three replicated RAMP designs (Section IV), two by the RAMP developers [4] and one by us (Section III). We then use Maude’s LTL model checker and the CAT tool [20] to analyze these specifications against data consistency properties such as the crucial RA that RAMP was built on and the prevalent session guarantee, called read your writes [28]. Our model checking results show that our own design satisfies all expected consistency properties (Section V).
A second key contribution is the uncovering of our promising design with highly desirable performance compared to those proposed by the RAMP developers. To do so, we further transform the above untimed, non-probabilistic, and nondeterministic Maude models that are used for standard model checking w.r.t. logical properties into timed and purely probabilistic models for statistical model checking (SMC) [27], [31] w.r.t. performance properties. We subject the three designs to realistic transaction workloads with a wider range of experimental parameters. Our SMC analysis results shows that our own design incurs less transaction latency than the other designs under all experimented workloads (Section VI).

II. PRELIMINARIES

A. RAMP Transactions

To improve scalability and availability, large-scale cloud databases divide data into partitions that can be managed and accessed separately. Nonetheless, providing strong consistency guarantees for multi-partition transactions typically incurs high latency. Thus, trade-offs that combine efficiency with weaker transactional guarantees for such transactions are needed.

Bailis et al. [4] propose a database isolation model, called read atomicity (RA), and Read Atomic Multi-Partition (RAMP) transactions, providing efficient multi-partition operations guaranteeing RA. For instance, in a social networking scenario, if Batman and Robin become “friends” in one transaction, then other transactions should not see that Robin is a friend of Batman but that Batman is not a friend of Robin: Either both relationships are visible to others or neither is.

Three RAMP algorithms, RAMP-Fast, RAMP-Small, and RAMP-Hybrid, are proposed in [4], offering different trade-offs between the size of a message payload and performance. We focus on RAMP-Fast as both design strategies for replicating RAMP transactions (Section II-B), as well as our own design alternative (Section III), are based on it.

**RAMP Writes:** To guarantee that all partitions perform a transaction successfully or that none do, RAMP performs two-phase writes by using the two-phase commit protocol (2PC): In the prepare phase, each timestamped write is sent to its partition, which adds the write to its local database. In the commit phase, each partition updates an index which contains the highest-timestamped committed version of each item.

**RAMP Reads:** Read transactions proceed by first fetching the highest-timestamped committed version of each requested data item (or key) from the corresponding partition (by the first-round get message), and then deciding if they have missed any version that has been prepared but not yet committed. The timestamp and the metadata from each version read produces a mapping from items to timestamps that represent the highest-timestamped write for each transaction, appearing in the first-round read set. If the reader has a lower timestamp version than indicated in the mapping for that item, a second-round read (or get message) will be issued to fetch the missing version. Once all the missing versions have been fetched, the client can return the resulting set of versions, which include both the first-round reads as well as any missing versions fetched in the second-round reads.

B. Replicating RAMP Transactions

Replication is critical for improving data availability and system fault tolerance. However, the RAMP algorithms [4] do not take data replication into account. The paper [4] briefly discusses two design strategies for replicating RAMP transactions in a multi-datacenter/cluster setting, where database partitions are located in separate clusters in possibly geo-graphically remote regions. Nonetheless, only high-level designs are provided without any concrete algorithm or formal analysis.

**Prepare-F HA RAMP (PHR):** A client sets a minimum durability for its writes, i.e., the number of failures $F$ it wishes to survive. When writing, the client issues a prepare request to all clusters and waits until it receives a successful response from $F+1$ partitions before starting to commit the transaction. Once all partitions have received the prepare request via, e.g., an asynchronous callback on the client, they commit the writes autonomously.

**Sticky HA RAMP (SHR):** Each client is assigned to its own cluster. Instead of issuing prepare and commit requests to all database replicas, the client issues them to its assigned cluster before forwarding them to other clusters for replication. The client can commit the transaction once it has performed the RAMP protocol only in its local cluster.

C. Rewriting Logic, Maude, and PVeStA

**Rewriting Logic and Maude.** Maude [9] is a rewriting-logic-based executable formal specification language and high-performance analysis tool for object-based distributed systems. A Maude module specifies a rewrite theory [23] $(\Sigma, E \cup A, R)$, where:

- $\Sigma$ is an algebraic signature, i.e., a set of sorts, subsorts, and function symbols.
- $(\Sigma, E \cup A)$ is a membership equational logic theory [9], with $E$ a set of possibly conditional equations and membership axioms, and $A$ a set of equational axioms such as associativity, commutativity, and identity, so that equational deduction is performed modulo the axioms $A$.
- The theory $(\Sigma, E \cup A)$ specifies the system’s states as members of an algebraic data type.
- $R$ is a collection of labeled conditional rewrite rules $[l] : t \rightarrow t'$ if cond, with $l$ the label, that specify the system’s local transitions.

Equations and rewrite rules are introduced with, respectively, keywords eq, or ceq for conditional equations, and rl and crl. An equation $f(t_1, \ldots, t_n) = t$ with the owise (“otherwise”) attribute can be applied to a subterm $f(\ldots)$ only if no other equation with lefthand side $f(u_1, \ldots, u_n)$ can be applied. Maude also provides standard parameterized data types (sets, maps, etc.) that can be instantiated (and renamed). For example, $\text{pr \ SET}(\text{Nat}) \ast (\text{sort \ Set}(\text{Nat}) \to \text{Nats})$ defines a set of natural numbers of sort Nats.
A class declaration class C | att\(_1\) : s\(_1\), ..., att\(_n\) : s\(_n\) declares a class C of objects with attributes att\(_1\) to att\(_n\) of sorts s\(_1\) to s\(_n\). An object instance of class C is represented as a term <O : C | att\(_1\) : val\(_1\), ..., att\(_n\) : val\(_n\)>, where O, of sort_oid, is the object’s identifier, and where val\(_1\) to val\(_n\) are the current values of the attributes att\(_1\) to att\(_n\). A message is a term of sort Msg. A system state is modeled as a term of the sort Configuration, and has the structure of a multiset made up of objects and messages.

The dynamic behavior of a system is axiomatized by specifying each of its transition patterns by a rewrite rule. For example, the rule (with label 1)

\[
\text{rl [1] : } m(O, w) \rightarrow <O : C | a1 : x, a2 : O', a3 : z > \text{ if } cond(O, x, a2, a3) \text{ with probability } \pi(O', x).
\]

defines a family of transitions in which a message m(O, w) is read and consumed by an object O of class C, whose attribute a1 is changed to x and a new message m'(O', x) is generated. Attributes whose values do not change and do not affect the next state (e.g., a3) need not be mentioned in a rule.

Statistical Model Checking and PVeStA. Probabilistic distributed systems can be modeled as probabilistic rewrite theories [2] with rules of the form

\[
[1] : t(\overrightarrow{x}) \rightarrow t'(\overrightarrow{x}, \overrightarrow{y}) \text{ if } cond(\overrightarrow{x}) \text{ with probability } \pi(\overrightarrow{x})
\]

where the term t' has additional new variables \(\overrightarrow{y}\) disjoint from the variables \(\overrightarrow{x}\) in the term t. For a given matching instance of the variables \(\overrightarrow{x}\) there can be many ways to instantiate the extra variables \(\overrightarrow{y}\). The values of these variables \(\overrightarrow{y}\) are sampled according to the probability distribution \(\pi(\overrightarrow{x})\), which depends on the matching instance of \(\overrightarrow{x}\).

Statistical model checking [27], [31] is a formal approach to analyzing probabilistic systems against temporal logic properties. It can verify a property up to a user-specified level of confidence by running Monte-Carlo simulations of the system model. In this paper we use the PVeStA tool [3] to statistically model check purely probabilistic systems against properties expressed by QUATEX formulas [2].

A timestamp is modeled as a pair \((K, T)\) consisting of the key, its value, and the version’s timestamp and metadata. A timestamp is modeled as a pair \(<id, sqn>\) consisting of an object identifier and a local sequence number that together uniquely identify a version. Metadata are modeled as a set of keys, indicating, for each key, the sibling keys written in the same transaction. For example, if a transaction writes keys \(k_1, k_2, k_3\), then the sibling keys of \(k_1\), as the metadata, are the set \({k_2,k_3}\).

Classes and Objects. A partition stores parts of the entire database. We formalize it as an object instance of the following class Partition:

```
class Partition | versions : Set{Version},
                latestCommit : Map{Key, Timestamp}.  
```

where the partitioned database consists of a set of versions for each key stored locally. The partition also retains the timestamp of the latest committed version for each key.

A transaction is modeled as an object instance of class Txn:

```
class Txn |
```

Terms of timestamped versions prior to the first-round reads. Specifically, the client maintains, for each key \(K\), the last seen timestamp \(T_{ls}\) and associated timestamp \(T_{md}\) for the metadata (i.e., sibling keys). Requesting the version with the maximum of \(T_{ls}\) and all those \(T_{mds}\) where \(K\) is a sibling key always guarantees RA. The client can run a periodic stabilization protocol to update \(T_{ls}\) and \(T_{md}\) for each key, or piggyback all information via regular RAMP messages.

Since each read in SHR-Faster needs only one RTT, it should incur lower transaction latency than the other replication designs. Regarding data consistency, SHR-Faster is expected to guarantee the essential read atomicity, as well as an important session guarantee, called called read your writes (RYW) [28], advocated by many industrial database applications [8]. With all these interesting properties, SHR-Faster would be an attractive option for replicating read atomic multi-partition transactions where RA, RYW, and low latency are highly desired.

IV. FORMALIZING DESIGNS

Designs are formalized in an object-oriented style, where the state is a multiset consisting of a number of partition objects, each modeling a partition of the entire database, a number of client objects, each executing transactions formalized also as objects residing inside the client, and a number of messages traveling between the objects. Regarding system dynamics, we focus on the designs’ differences. The entire executable Maude specifications are available at [1].

A. Data Types, Objects, and Messages

Basic Data Types. A version is modeled as a 4-tuple <key, value, timestamp, metadata> (of sort Version) consisting of the key, its value, and the version’s timestamp and metadata. A timestamp is modeled as a pair <id, sqn> consisting of an object identifier and a local sequence number that together uniquely identify a version. Metadata are modeled as a set of keys, indicating, for each key, the sibling keys written in the same transaction. For example, if a transaction writes keys \(k_1, k_2, k_3\), then the sibling keys of \(k_1\), as the metadata, are the set \({k_2,k_3}\).

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```
class Partition | versions : Set{Version},
                latestCommit : Map{Key, Timestamp}.  
```

where the partitioned database consists of a set of versions for each key stored locally. The partition also retains the timestamp of the latest committed version for each key.

A transaction is modeled as an object instance of class Txn:

```
class Txn |
```
where the attribute operations denotes the transaction’s operations, with each of the form read(key) or write(key, value). The attribute readset, resp. writestset, denotes the <key, value> pairs fetched, resp. written, by the read, resp. write, operations of the transaction. The attribute votes stores the votes from the partitions which participate in the 2PC protocol. The remaining attributes commits, 1stReads, and 2ndReads store, respectively, the partitions from which the client is awaiting committed commits which participate in the 2PC protocol. The remaining attributes votes, 2ndReads, and 2ndReads store, respectively, the partitions from which the client is awaiting committed

A client, modeled as an object instance of class Client, is delegated to process transactions:

class Client |  
  queue : List{Object}, executing : List{Object},  
  dc : Oid, last : Map{Key,Timestamp} .

The attributes queue, executing, and committed store the transaction(s) which are waiting to be executed, currently executing, and committed, respectively. Concurrently executing transactions can be modeled by multiple clients with each holding a currently executing transaction. The attribute dc refers to the datacenter where the client is co-located. The attribute last, specific to SHR-Faster, maps each key to the pair <timestamp, metadata> of its latest version that the client has seen.

The state also contains a “table” object of class Table mapping each key to the partitions storing the key (called the key’s replicas), and each datacenter to its partitions.

The following shows an example initial state of sort Configuration (with some parts replaced by ‘...’ with two clients, c1 and c2, queuing, respectively, two and one transactions. Read transaction t1 has two read operations on, respectively, two keys k1 and k2. Write transaction t2 consists of two write operations, with each writing a value (e.g., ”TASE”) to a key (e.g., k2). Transaction t3 is a transaction of a single read on key k4. The key space is split by two partitions p1 (resp. p3) and p2 (resp. p4) and replicated in two datacenters, e.g., key k1 is replicated at partitions p1 and p4 that are located in datacenters d1 and d2, respectively. Each partition is initialized accordingly; in particular, for each key, the value is the empty string, the timestamp is null, and the metadata is an empty set:

```
operations : List{Operation}, txnSqn : Nat,  
votes : Set{Oid}, commits : Set{Oid},  
1stReads : Set{Oid}, 2ndReads : Set{Oid},  
latest : Map{Key,Timestamp},  
readset : Set{kvPair}, writestset : Set{kvPair} .
```

Messages. A message has the form (to receiver from sender : mc). The terms sender and receiver are object identifiers. The term mc is the message content, having the form of either get(txn, key, ts, dc), a get message, sent to the corresponding partition located in datacenter dc, requesting key’s version with the timestamp ts; reply(txn, key, val, ts, md), the returned version from the partition for first-round get request; prepare(txn, key, val, ts, md, dc), the version sent from a write transaction to the corresponding partition in datacenter dc; vote(txn, vote), the reply to the corresponding prepare message where vote denotes the partition’s decision on whether it can commit the transaction; commit(txn, ts, dc), the demand for committing the version with timestamp ts; or ack(txn), the acknowledgment of committing the transaction from the partition. Note that SHR-Faster only use reply messages for transaction reads as no second-round read is needed.

B. Formalizing System Dynamics

We have formalized the dynamic behaviors of all three designs using rewrite rules. In this section we focus on the core difference (denoted by the colored parts in italics in a rule), that typically lies in the client-side methods, between PHR and SHR w.r.t. processing write transactions, and between SHR and SHR-Faster w.r.t. processing reads.1 We exemplify each case with one rule, and refer to [1] for the remaining rules including the partition-side methods.

1) Processing Writes: The following rule shows how an SHR client proceeds once the prepare phase ends (checked by all the predicate if all vote messages have been received):

```
crl [rcv-vote-shr] :  
{from O’ to O : vote(TID, yes)}  
< T : Table | replicas : RS, cluster : DS >  
< O : Client | dc : DC, executing :  
  < TID : Txn | operations : OPS, txnSqn : N,  
  votes : VS, commits : CS > } =>  
  < T : Table | >  
< O : Client | executing :  
  < TID : Txn | votes : VS’, commits : CS,  
  < p1 : Partition | versions : (k1, null, empty >,  
  < p2 : Partition | ... > } >  
  addCommitsOneDc(OPS, RS, DS, DC)  
  if all(VS’) then else empty fi > >  
  (if all(VS) then genCommitsOneDc(0, TID, N, OPS, RS, DS, DC)  
  else none fi)  
  if VS’ := remove(O’, VS) .
```

1We do not include variable declarations, but follow the Maude convention that variables are written in (all) capital letters.
The client starts to commit the executing transaction by generating the commit messages for all the participating datacenters involved in the 2PC protocol (by the genCommitsOneDc function). The addCommitsOneDc function computes the corresponding partitions of the participating datacenters. The remove function updates the client’s waiting list for votes.

Modifications for PHR. Instead of all votes in the co-located cluster, a PHR client collects a majority of responses (checked by the quorum predicate) from all replicas, including remote ones, before propagating the commit messages (by the genCommitsAllDc function):

crl [rcv-vote-phr] :
   (from O’ to O : vote(TID,yes))
   < T : Table | replicas : RS, cluster : DS >
   < O : Client | dc : DC, executing :
   < T : Table | operations : OPS, txnSqn : N,
   votes : VS, commits : CS >
   committed : TXNS, dc : DC >
=>
   < T : Table | >
   (if quorum(VS'))
   then < O : Client | executing : empty,
   committed : (TXNS
   < T : Table | votes : VS', commits : (CS,
   genCommitsAllDc(OPS,RS,DS,DC)) >) >
   genCommitsAllDc(O,TID,N,OPS,RS,DS,DC)
   else < O : Client | executing :
   < T : Table | votes : VS' > fi)
if VS' := remove(O',VS) .

The corresponding replicas are added to commits, from which the client waits for the ack messages. Notice that, unlike SHR, PHR then commits the transaction by moving it from executing to committed; the client can therefore issue the next transaction in the queue.

2) Processing Reads: The key difference between SHR and its optimization SHR-Faster lies in how a client reacts to the first-round reads. In SHR, upon receiving a reply, the client checks whether all first-round responses have been collected (by the all predicate): the client then issues second-round get messages (by gen2ndReads) if any writes are missing; otherwise, it continues to wait for the remaining first-round reply messages:

crl [rcv-1st-reply-shr] :
   (from O’ to O : reply(TID,K,V,TS,MD))
   < T : Table | replicas : RS, cluster : DS >
   < O : Client | dc : DC, executing :
   < T : Table | operations : OPS, readset : RS,
   latest : VL, 1stReads : 1ST, 2ndReads : 2ND >
=>
   < T : Table | >
   < O : Client | dc : DC, executing :
   < T : Table | readSet : (RS', latest : VL',
   1stReads : 1ST', 2ndReads : 2ND, 2ndPars(VL',RS',RS,DS,DC)
   (if all(1ST') then
   2ndPars(VL',RS',RS,DS,DC)
   else empty fi) >
   (if all(1ST') then
   gen2ndReads(O,TID,VL',RS',RS,DS,DC)
   else none fi)
if RS' := RS, < K,V,TS,MD > \ VL' : lat(VL,MD,TS)
/ \ 1ST' := remove(O',1ST) .

The 2ndPars function computes the corresponding partitions (possibly none) involved in the second-round communication. The lat function updates the current key-timestamp mappings VL with the latest committed timestamp received (i.e., TS), which are then used to compute the missing writes. The client also updates its readset accordingly (i.e., RS').

The SHR client commits a read transaction (moved from executing to committed) if both 1stReads and 2ndReads are empty, indicating that all first- and second-round replies have been received:

crl [rcv-1st-reply-shr-faster] :
   (from O’ to O : reply(TID,K,V,TS,MD))
   < O : Client | last : KP, committed : TXNS,
   executing :
   < TID : Txn | last : last(KP,< K,V,TS,MD >),
   committed : (TXNS
   < TID : Txn | readset : (RS, < K,V,TS,MD >),
   1stReads : remove(O',1ST') >),
   executing : empty >
else
   < O : Client | executing :
   < TID : Txn | readset : (RS, < K,V,TS,MD >),
   1stReads : remove(O',1ST') > fi .

where, unlike SHR, no second-round get request is generated. The client also updates last with the received version for computing RA-consistent snapshots of the database (see [1] for details).

V. MODEL CHECKING CORRECTNESS PROPERTIES

This section shows our formal analysis of all three designs against three data consistency properties using the CAT tool [20] and Maude’s built-in model checker. In particular, we formalize in Maude the read your writes session guarantee which CAT cannot handle.

A. The CAT Model Checker

CAT [20] is a Maude-based tool for model checking data consistency properties of distributed transaction systems like SHR specified in Maude. It currently supports nine transactional consistency properties, including RA and the weaker consistency property read committed (RC) used as the default isolation level by almost all SQL databases [11].

B. Formalizing Read Your Writes

Read your writes [28] guarantees that the effects of all writes performed by a client are visible to its subsequent reads. We define RYW in Maude as a predicate over states as follows:
The predicate `ryw` analyzes RYW by checking (the state) whether there was a “bad situation” in which a committed transaction had fetched an RYW-`inconsistent` value. More specifically, we consider three such cases:

1) Instead of returning the previous write in the same session, a committed transaction `TID3` reads an even earlier write (by matching the key `K` and the value `V`) in the same session (the first equation).

2) A committed transaction `TID3` fetches a write from a different session, which has an earlier version than `TID3`’s previous write in the same session (the second conditional equation).

3) Despite a previous write in the same session, a committed transaction `TID2` returns the initial value (the third equation).

The fourth equation covers all the remaining (RYW-consistent) cases. Note that `CONF` (of sort `Configuration`) denotes the rest of the entire configuration (or state) in the first three equations.

### C. Model Checking Analysis

We have applied CAT and Maude’s built-in model checker to three Maude models of the designs against RA, RC, and RYW, respectively.

<table>
<thead>
<tr>
<th>Maude Model</th>
<th>LOC</th>
<th># rules</th>
<th>Consistency Property</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td></td>
<td>RC</td>
</tr>
<tr>
<td>PHR</td>
<td>845</td>
<td>14</td>
<td>✓</td>
</tr>
<tr>
<td>SHR</td>
<td>894</td>
<td>14</td>
<td>✓</td>
</tr>
<tr>
<td>SHR-Faster</td>
<td>887</td>
<td>12</td>
<td>✓</td>
</tr>
</tbody>
</table>

Table I summarizes our model checking results. All three designs satisfy RA, as well as RC. Regarding RYW, our analysis shows that only PHR does not satisfy the property. The counterexample obtained by analyzing the initial state where two clients `c1` and `c2`, each issuing two transactions, shows that the read operations from `c1` return the values written by `c2`’s first write transaction `write(k1,11) write(k2,54)` that was issued before `c1`’s first write transaction. The reason is that a PHR read transaction could access the versions written before its last write transaction commits; PHR enables “fast” commit of writes once the client collects a majority of responses from all the participants.

We have run CAT with automatically generated different initial states [20], with up to 6 transactions, 2 operations per transaction, 3 clients, 6 partitions, 3 datacenters, 3 keys, and 3 replicas per key. We have also employed these initial states in our analysis of RYW with Maude’s built-in model checker. Each analysis took about one hour (worst case) to execute on a 3.3 GHz Dual-Core Intel Core i7 CPU with 16GB memory.

### VI. Quantitative Analysis Using SMC

Our qualitative analysis in Section V investigates the desired data consistency guarantees—SHR-Faster, as well as SHR, satisfies all three properties.

SHR-Faster must therefore outperform SHR, as well as PHR, to be an attractive design. In this section we use statistical model checking with PVeStA to compare the performance of these designs in terms of average transaction latency.

#### A. Probabilistic Models

The models in Section IV are untimed, non-probabilistic, and nondeterministic, which can be analyzed w.r.t. their logical properties using model checking. To estimate the system performance, we need to enrich the models with time and probabilities and eliminate any nondeterminism. The transformed models are therefore timed and purely probabilistic, which can be subjected to SMC.

We follow the methodology in [2] by assigning to each message a delay sampled from a continuous probability distribution so that the probability that two messages have the same delay is 0. The framework [2] then guarantees no unquantified nondeterminism by firing a rewrite rule according to the arrival of a message. The elapse of message delays, as well as advancing the global clock, is maintained by a scheduler object in the framework.

We exemplify with a (partition-side) rule how we have transformed the untimed non-probabilistic rewrite rules to the timed and probabilistic setting. In the transformed probabilistic rule below, upon receiving the `prepare` message at global time `GT`, the partition stores the associated version `< K,V,TS,MD >` in its local database, and sends its vote `yes` back with message delay `D` sampled from probability distribution `distr(x)`:  

```plaintext
rl [rcv-prep-prob] : 
(GT, (to O' from O : prepare(TID,K,V,TS,MD,DC))) 
< O : Partition | versions : VS > 
=>
```

```plaintext
< TID1 | writeset : (< K,V,TS,MD >, WS) > TXNS2
<TID2 | writeset : (< K',V',TS',MD' >, WS') > TXNS3
<TID3 | readset : (< K,V,TS'',MD'' >, RS) > TXNS4
CONF = false

```

```plaintext
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Latency (time unit)
Percentage of Reads
SHR-Faster
SHR
PHR
(a)

Avg. Latency (time unit)
Key Access Distribution
SHR-Faster
SHR
PHR
(b)

Avg. Latency (time unit)
Transaction Size (operations)
SHR-Faster
SHR
PHR
(c)

Fig. 1. Statistical model checking analysis results for the comparison of three designs.

\(< O : \text{Partition | versions : (VS, < K,V,TS,MD >)} >
\[D, (\text{to } O' \text{ from } O : \text{vote}(TID,\text{yes}))\] with probability \(D := \text{distr}(x)\).

where \text{distr} is parametric on \(x\), the corresponding variables in the lefthand side of the rule (see [20] for details). The outgoing \text{vote} must then be consumed by receiver \(O'\) when time \(D\) elapses, i.e., at global time \(GT + D\).

B. Extracting Transaction Latency Measures

PVeStA estimates the expected value of a QuaTEx expression on a run, up to a desired statistical confidence. Hence, the key to performing SMC is to define a measure on system runs. We then define a function on states that extracts the latency metric from the system execution log recorded by a monitor object (similar to the monitor defined in CAT [20]; see Section V). Specifically, the monitor stores important information about each transaction, i.e., its ID, issue time, and commit time. Thanks to the transformed rules, we can extract timing information, e.g., the current global time, directly from an incoming message (see rule \text{rcv-prep-prob} above). We have modified the probabilistic models by updating the monitor object whenever needed. See [1] for details.

C. Benchmark and Experimental Setup

To statistically analyze the designs’ performance, we implement in Maude a parametric workload generator that probabilistically generates a different initial state for each simulation in an SMC analysis. The parameters are: \#clients (default: 50), \#clusters (default: 3), \#partitions/cluster (default: 5), \#keys (default: 1k), \#transactions (default: 400), \#ops/transaction (default: 2), \%reads (default: 50), and key-access distribution\(^2\) (default: Zipfian [10]).

To mimic the real-world multi-datacenter environment, we use the lognormal distribution for probabilistically sampling message delays [5], which are further modulated linearly according to the distance between the sender and receiver. We employed 20 d430 Emulab machines [30], each with two 2.4 GHz 64-bit 8-Core E5-2630 processors, to parallelize SMC with the PVeStA tool [3]. We set the statistical confidence level to 95% and the size parameter to 0.01 for all our experiments.

\(^2\)Key-access distribution is the probability that a read/write operation accesses a certain data item.

D. SMC Analysis Results

We have subjected the transformed purely probabilistic models to the above workload generator and PVeStA, and performed three sets of experiments on measuring average latency. Each SMC analysis took up to two hours (worst case) to terminate. Each point in the plots represents the average of three SMC results.

Fig. 1 depicts the average latency as a function of percentage of reads, key-access distribution, and transaction size, respectively. The plots show that our SHR-Faster design outperforms SHR, which in turn outperforms PHR, for all parameter combinations.

As shown in Fig. 1-(a), the latency for PHR tends to decrease significantly, starting from 10% reads, with increasing reads in the mixed workload. The reason is that transactional writing must wait for \(F + 1\) (in this case 2) responses from the corresponding partitions, including at least one in the remote cluster, while reads need not to due to the weak consistency guarantee of read atomicity. The latency difference between SHR-Faster and SHR becomes larger with more concurrent writes (i.e., 50%–70% reads) as more second-round reads were issued to fetched the missing writes in SHR.

Fig. 1-(b) plots the comparison under various key-access distributions. With more frequent key accesses, i.e., Zipfian and hotspot (80% operations on 20% keys [10]), the latency difference is quite large as more second-round reads were sent to possibly remote partitions. The same argument applies to Fig. 1-(c) where increasing transaction size (i.e., \#ops/transaction) leads to more remote communications.

VII. RELATED WORK

Maude for RAMP. In [17] we formalized RAMP and its variants and used Maude model checking to analyze their correctness properties. In [14] we modeled RAMP and its extensions in probabilistic rewrite theories and employed SMC to compare their performance. None of these RAMP-family algorithms considers data replication that is indispensable in modern distributed database systems. In contrast, this paper focuses on replicated RAMP transactions and also introduces our most promising replication design SHR-Faster. Moreover, this paper follows a more general methodology based on formal modeling with rewrite rules that are further transformed into probabilistic rewrite rules so that both qualitative and quantitative properties are investigated.
Maude for Distributed Databases. Existing work [12], [18], [19], [26] specifies and model checks various distributed transaction systems that provide other types of data consistency properties, as opposed to read atomicity and read your writes considered in this paper. The paper [12] estimate Google’s Megastore using randomized Real-Time Maude simulations. However, this methodology cannot offer any measure of statistical confidence in the estimations. The papers [13], [21] show how the NoSQL key-value store Cassandra has been formally analyzed for both data consistency and performance properties using Maude and PVeStA. Cassandra only supports single read/write operation, while transactional consistency properties such as RA are more complex to be analyzed.

Formal Methods for Distributed Databases. Other formal methods have been used in the design of distributed databases. One representative is TLA+ and its model checker TLC that have been used in both industry, e.g., Amazon’s cloud computing infrastructure [25], and academia, e.g., the TAPIR protocol [32]. In contrast to our work, they employ formal methods only for correctness checking but could not run any protocol [32]. We have explored in this paper three designs for replicated RAMP transactions by formal modeling with Maude rewrite rules and probabilistic rewrite theories, and by the analysis with standard model checking for data consistency properties and PVeStA statistical model checker for performance measurements, respectively. Substantial knowledge has been obtained about the design space. In particular, we have identified a promising design with sticky clients and one round-trip communication for transactional reads. We have shown that our design not only provides the crucial RA and RYW consistency guarantees, but also outperforms the other design alternatives w.r.t. transaction latency under various workloads.

A natural next step is to confirm our model-based SMC predictions of the designs with their implementation-based evaluations under the actual deployment in the cloud.

REFERENCES