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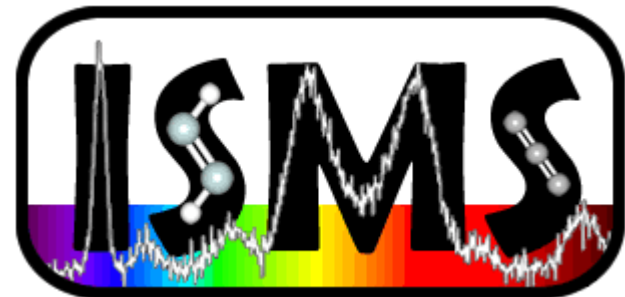
# High-precision mid-IR molecular spectroscopy with traceability to primary frequency standards using sub-Hz frequency comb-stabilized QCLs

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# Precision measurements with molecules

- Complementary to measurements in atoms for precision tests of fundamental physics:

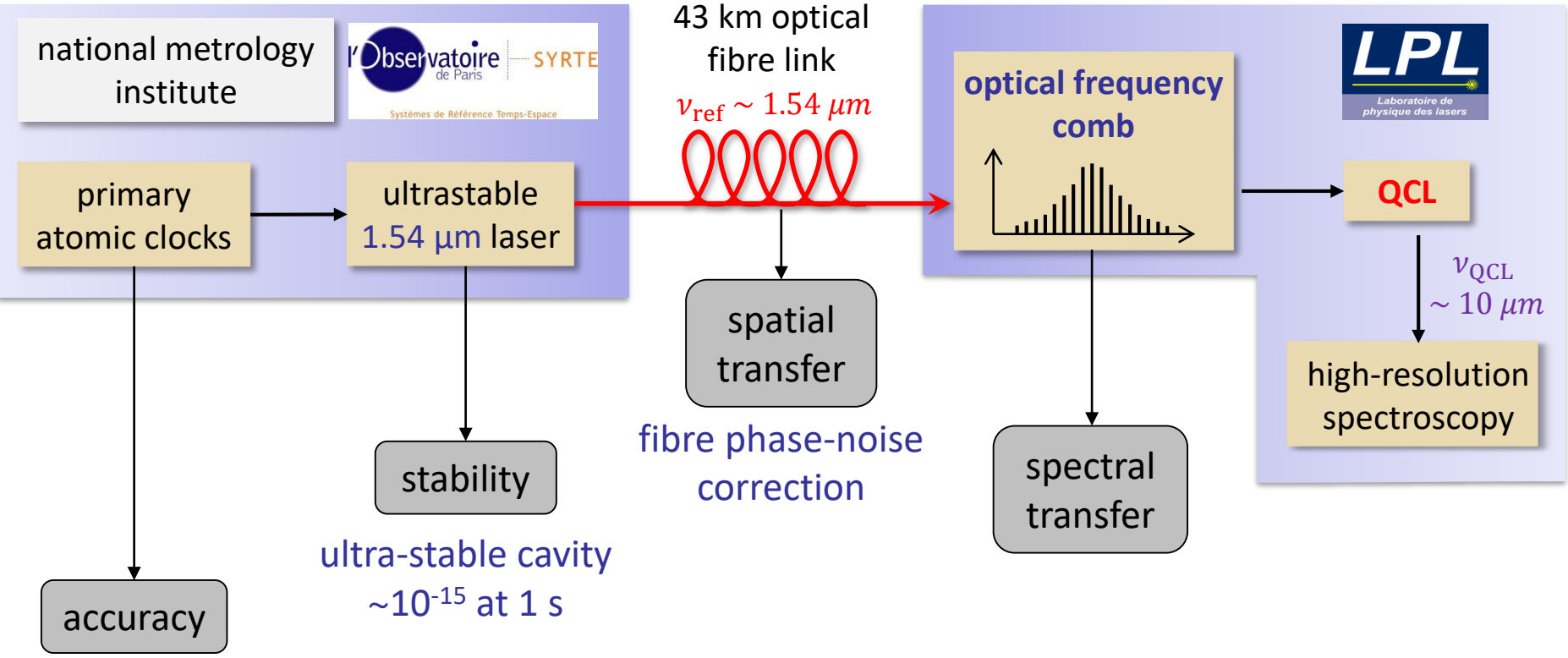
measure constants	$m_e/m_p$ (Schiller, Ubachs, Hilico – HD <sup>(+)</sup> , H <sub>2</sub> <sup>(+)</sup> ) $k_B$ (Gianfrani, H <sub>2</sub> O - LPL, NH <sub>3</sub> ),...
measure their variations in time	$\alpha$ (J. Ye, OH) $m_e/m_p$ (De Natale, Maddaloni, CF <sub>3</sub> H - LPL, SF <sub>6</sub> )
test parity & time-reversal symmetry (eEDM)	Hinds (YbF), DeMille/Doyle/Gabrielse (ThO),...
test parity symmetry	D. DeMille (BaF), LPL (chiral species),...
Test the symmetrization postulate	Tino, De Natale,... (O <sub>3</sub> , CO <sub>2</sub> , NH <sub>3</sub> ,...)

- Many are based on high-resolution spectroscopy, often in the mid-IR domain
- Increasing demand for precision spectroscopy of polyatomic molecules for physical chemistry studies:
  - modeling our atmosphere
  - interpreting astrophysical and planetary spectra
  - study collision physics
  - ...

# Precision measurements with molecules

- Need efficient **mid-IR laser sources** of **well-controlled frequency**
- Mid-IR **quantum cascade lasers (QCLs)** are promising
  - ✓ continuous-wave
  - ✓ available in the 3-25  $\mu\text{m}$  range
  - ✓ tuneability over several 100 GHz or more
  - ✓ mW to W power levels
  - ✗ free-running line width 10 kHz to few MHz  $\rightarrow$  frequency stabilization needed
- Several frequency stabilization schemes developed in the last years
  - $\rightarrow$  stable cavities, molecular lines, injection locking, optical frequency combs,...
- **Challenges:** achieve ultimate metrological frequency purity and accuracy traceability to *primary frequency standards* available *anywhere*
  - $\rightarrow$  use the best near-IR ultra-stable lasers found in metrology institutes as reference
  - $\rightarrow$  use ultra-stable optical fiber links
  - $\rightarrow$  use an optical frequency comb (OFC) to bridge the gap between near-IR and mid-IR

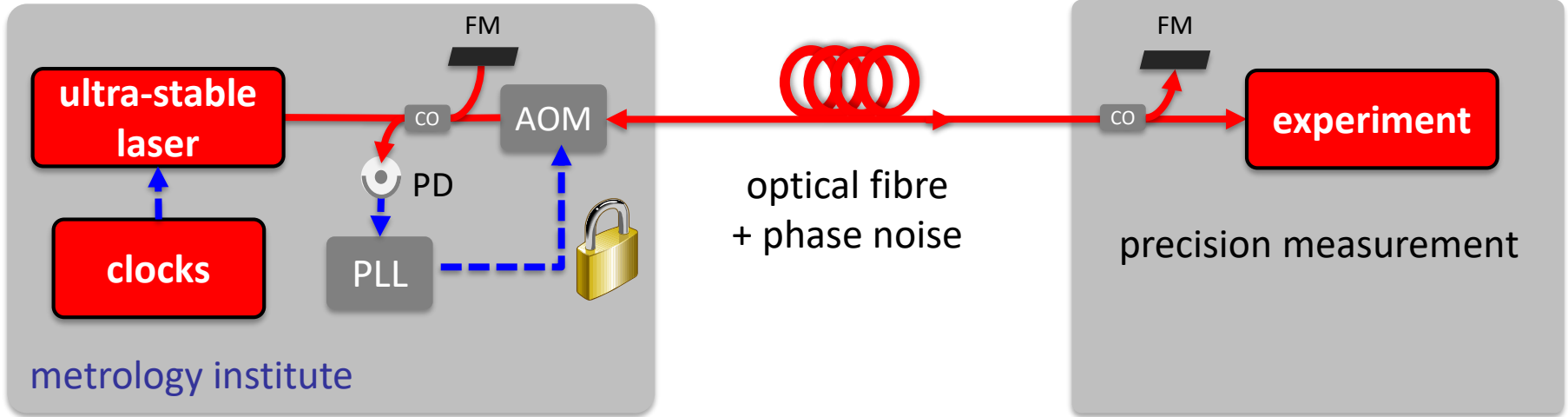
# QCL stabilization to a near-IR frequency reference



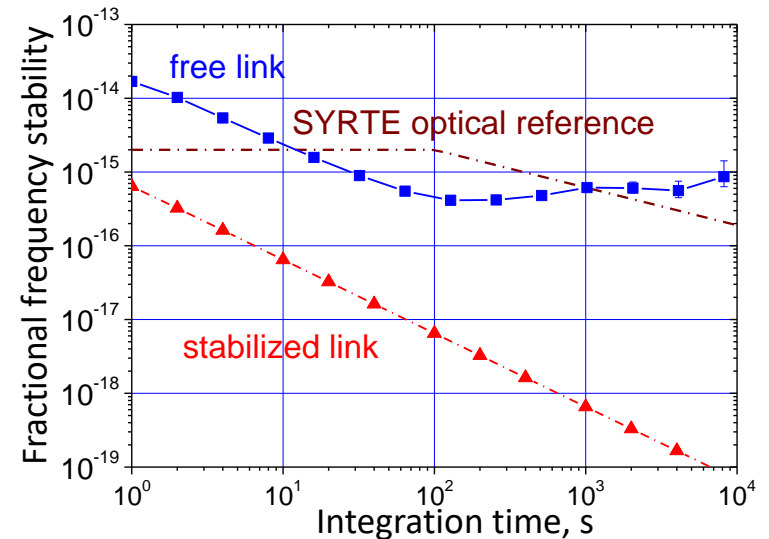
~10<sup>-14</sup> (H-maser)  
 ~10<sup>-16</sup> potentially (Cs fountain)

$$\nu_{\text{QCL}} = \frac{n}{N} (\nu_{\text{ref}} + \Delta_1) + \Delta_2$$

# Optical fibre link for ultra-stable frequency transfer



- correction of the propagation noise
- added noise (transfer instability)
  - a few  $10^{-16}$  after 1 s
  - $\sim 10^{-19}$  after  $\sim$ a day
- frequency inaccuracy  $< 10^{-19}$

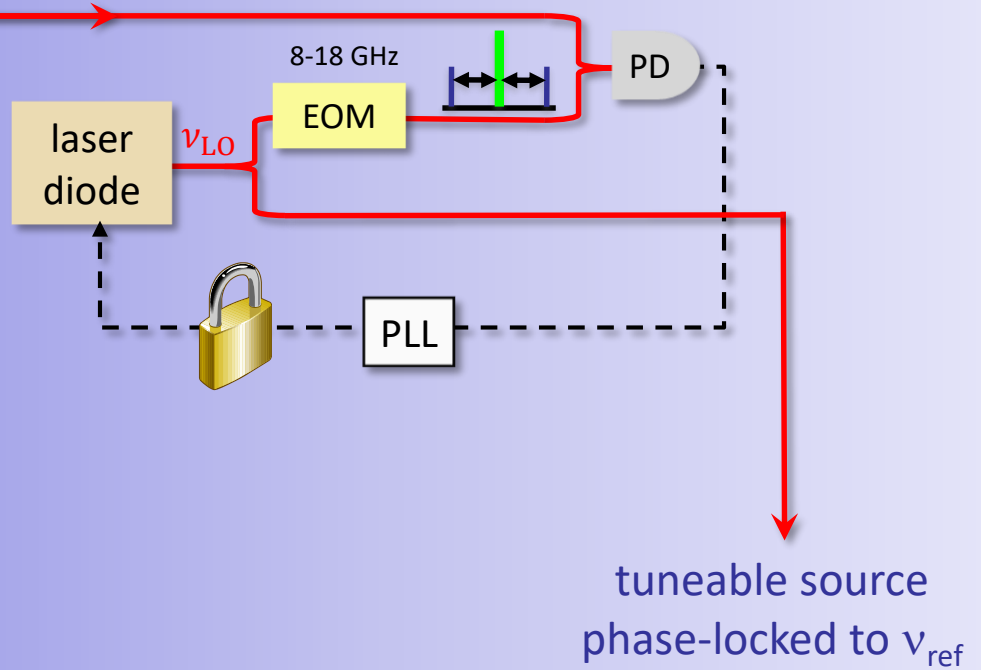


# QCL stabilization to a near-IR frequency reference

ultrastable  
1.54  $\mu\text{m}$  laser

43 km fibre

$\nu_{\text{ref}} \cong 1.54 \mu\text{m}$

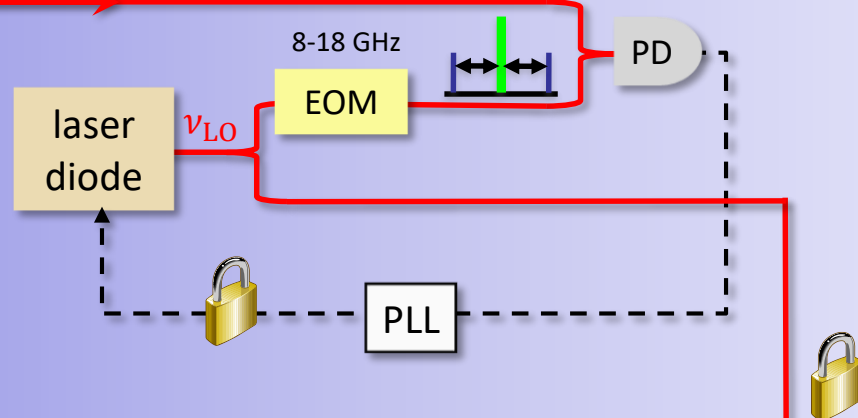


# QCL stabilization to a near-IR frequency reference

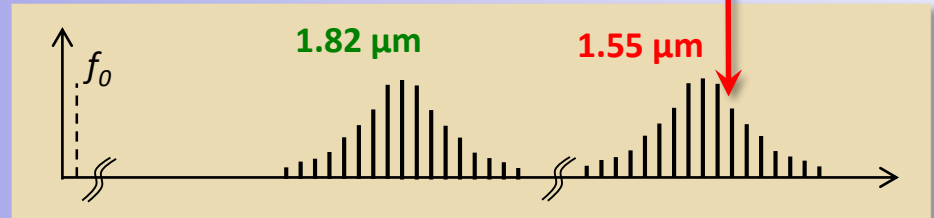
ultrastable  
1.54  $\mu\text{m}$  laser

43 km fibre

$\nu_{\text{ref}} \cong 1.54 \mu\text{m}$



- optical frequency comb :
  - 2 outputs
  - both stabilized
  - tuneable



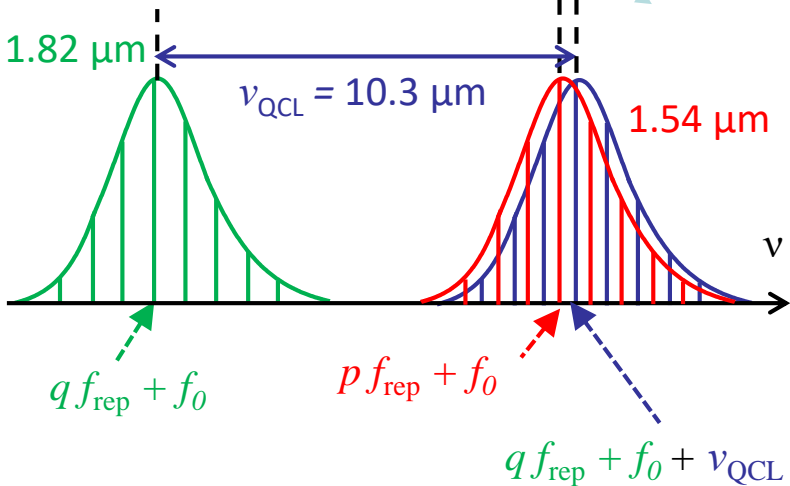
# QCL stabilization to a near-IR frequency reference

ultrastable  
1.54  $\mu\text{m}$  laser

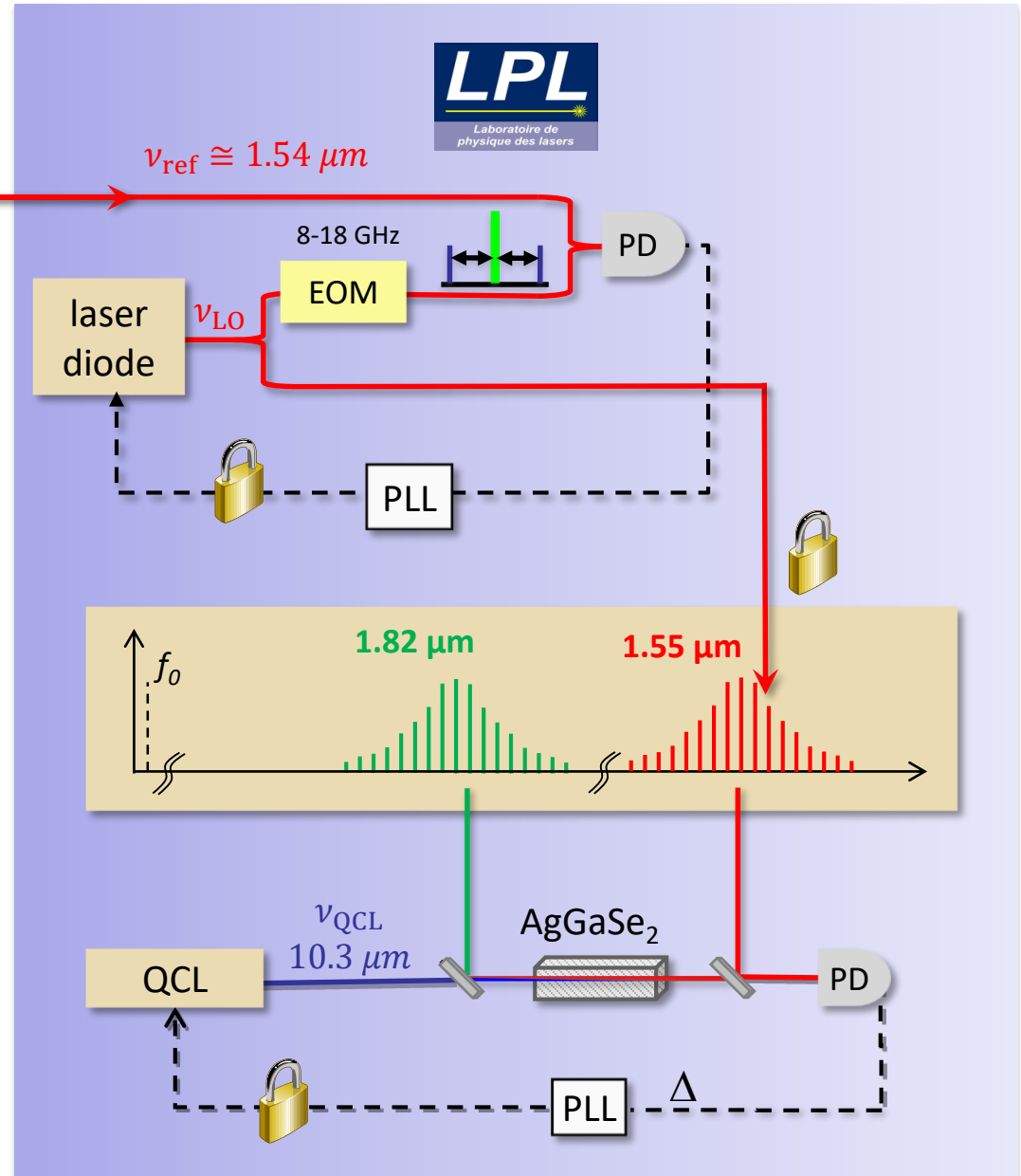


- sum frequency generation:

$$\Delta = (p-q) f_{\text{rep}} - \nu_{\text{QCL}}$$



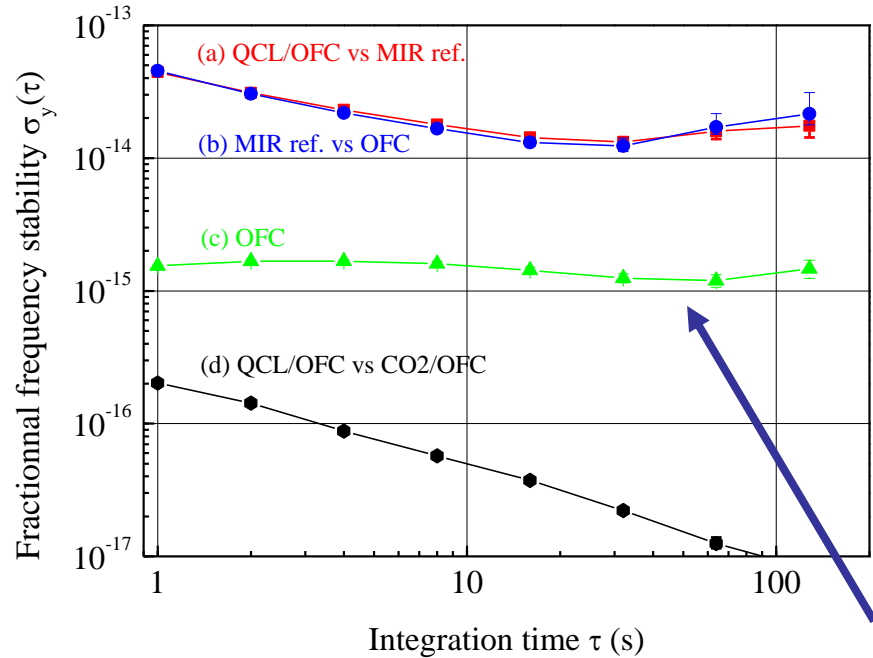
- direct link from near-IR and mid-IR
- QCL tuneable over  $\sim 1.5$  GHz



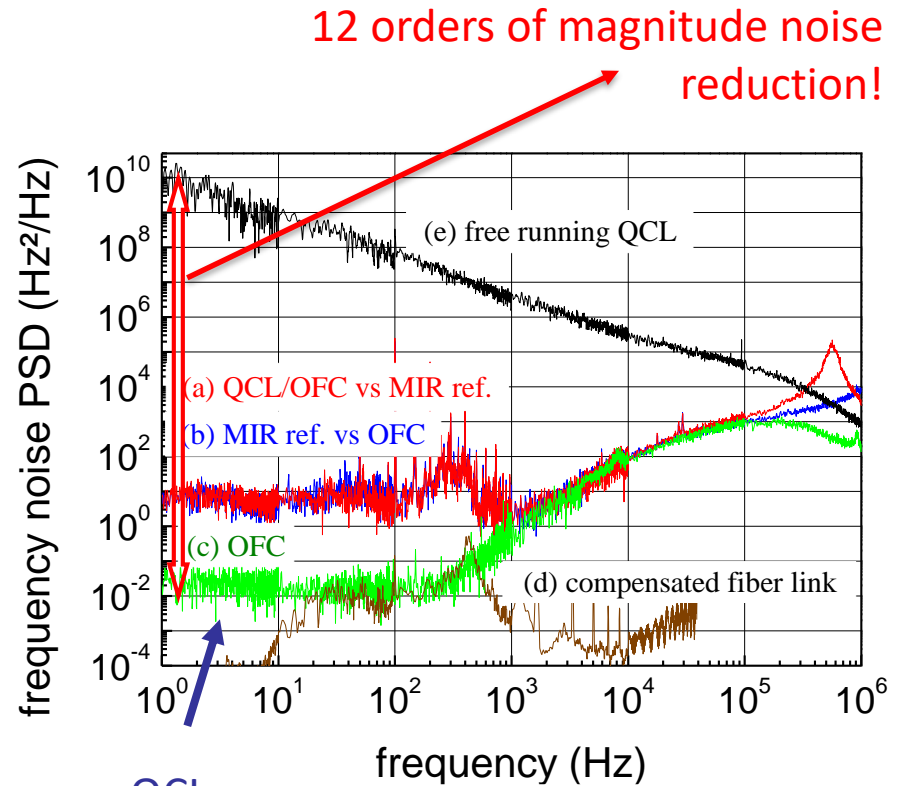


# Performances of the stabilized QCL

Argence et al, *Nature Photon.* (2015)  
 see also: Inero et al., *Sci. Rep.* (2017)



QCL  
stability



QCL  
noise

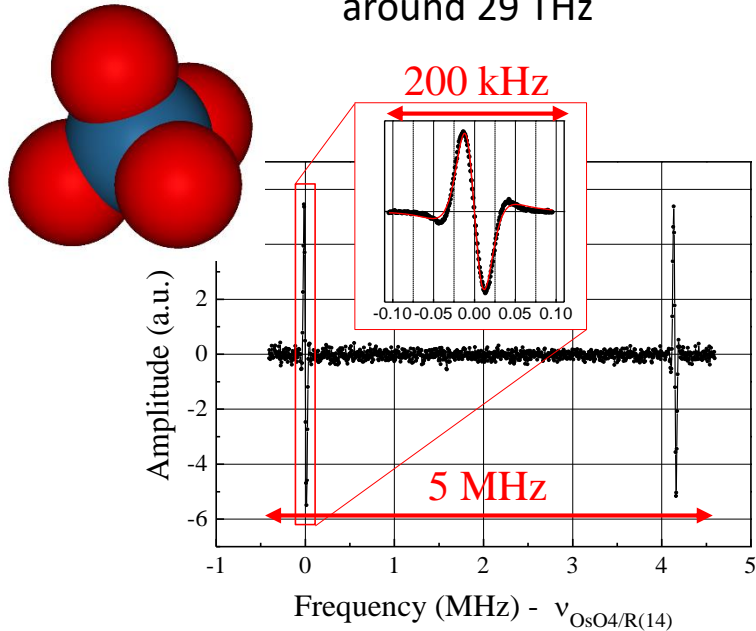
12 orders of magnitude noise  
reduction!

- ultimate QCL stabilities (0.06 Hz @ 1s) and accuracies (sub-Hz, 10 mHz potentially)
- narrowest QCL so far (0.1 Hz)

Allows the level of near-IR ultra-stable lasers to be transferred to the mid-IR  
 $\Rightarrow$  'atomic physics' types of precision measurements on molecules

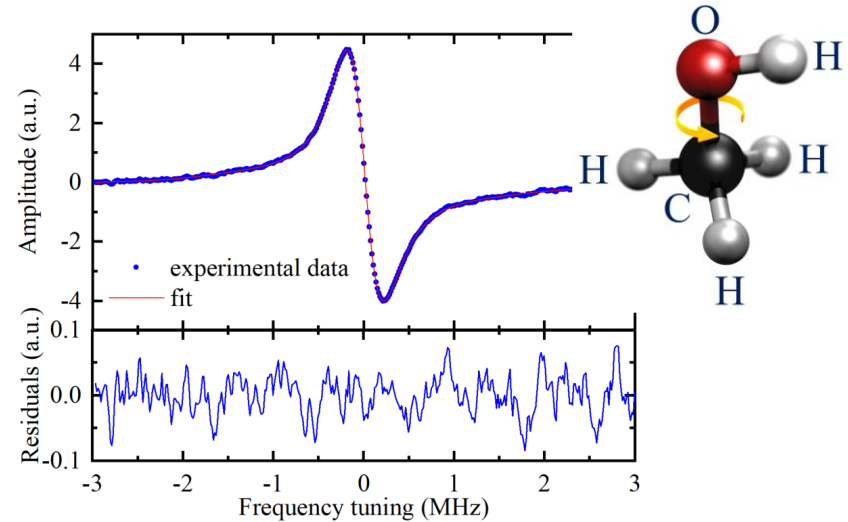
# Ultra-precise spectroscopy with quantum cascade lasers: record frequency uncertainties

OsO<sub>4</sub> saturated absorption spectrum  
around 29 THz



- ~25 kHz linewidth
- a few 10 Hz uncertainty
- state-of-the-art
- in a ~100 finesse 1.5-m long Fabry-Perot cavity
- frequency modulation 9.5 kHz, deviation 36 kHz
- 3<sup>rd</sup> harmonic detection, time constant: 5 ms

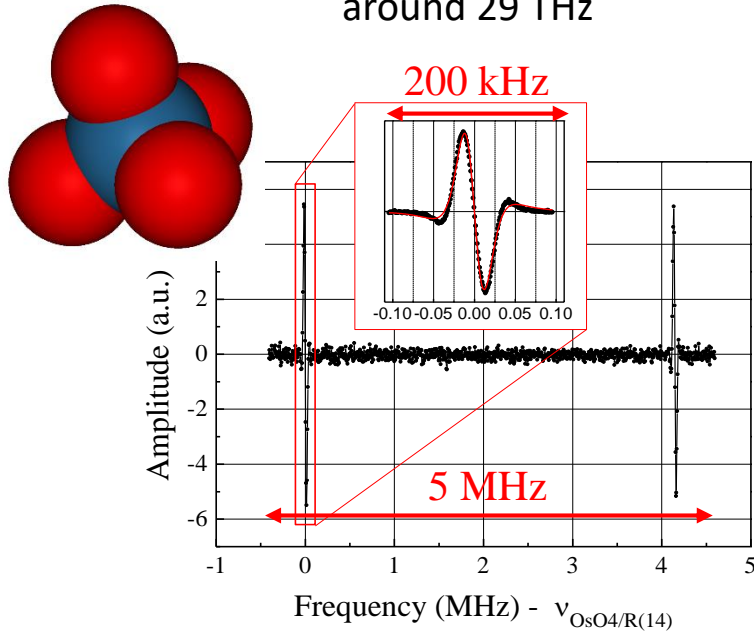
Methanol saturated absorption spectrum  
P(E<sub>1,co</sub>,0,2,32) line, C-O stretch



- ~400 kHz linewidth
- a few kHz uncertainty
- 10<sup>2</sup>-10<sup>4</sup> improvement compared to literature / HITRAN database
- in a multipass cell
- frequency modulation 20 kHz, deviation 50 kHz
- 1<sup>st</sup> harmonic detection, time constant: 100 ms

# Ultra-precise spectroscopy with quantum cascade lasers: record frequency uncertainties

OsO<sub>4</sub> saturated absorption spectrum  
around 29 THz



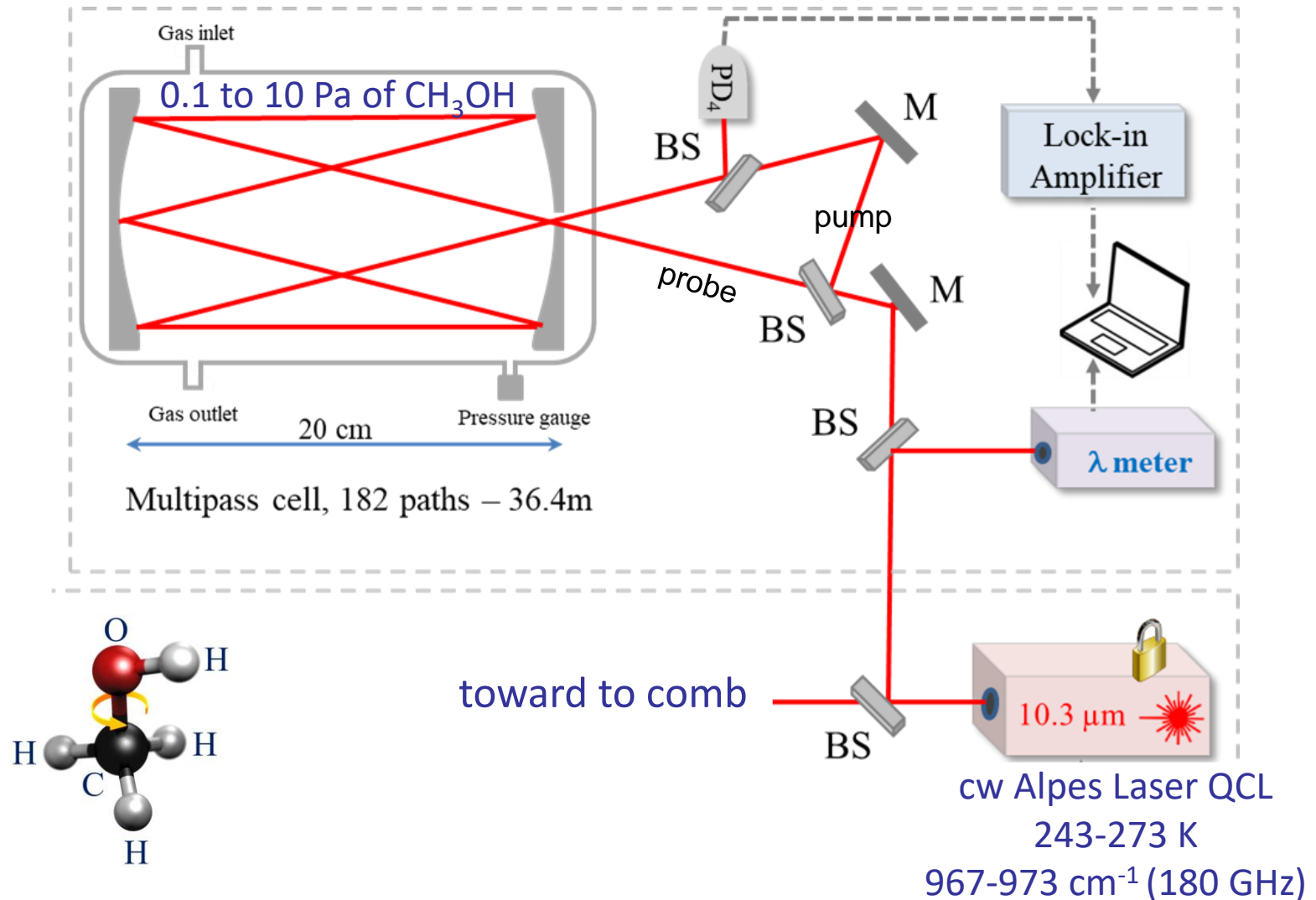
- ~25 kHz linewidth
- a few 10 Hz uncertainty
- state-of-the-art
- in a ~100 finesse 1.5-m long Fabry-Perot cavity
- frequency modulation 9.5 kHz, deviation 36 kHz
- 3<sup>rd</sup> harmonic detection, time constant: 5 ms

**Table 1 | Absolute frequencies of five OsO<sub>4</sub> absorption lines in the vicinity of the R(14) CO<sub>2</sub> laser line.**

OsO <sub>4</sub> lines in the vicinity of the CO <sub>2</sub> R(14) laser line at 10.3 μm	Frequency shift from $\nu_{\text{OsO}_4/\text{R}(14)}$ calculated from refs 39 and 41 (kHz)	Frequency shift from $\nu_{\text{OsO}_4/\text{R}(14)}$ measured in this work (kHz)
<sup>190</sup> OsO <sub>4</sub> reference line (unassigned)	0.000 (40)	-0.009 (22)
Unreported line	-	+4,147.399 (23)
<sup>190</sup> OsO <sub>4</sub> , R(46)A <sub>1</sub> <sup>3</sup> (-)	+101,726.83 (5)	+101,726.821 (32)
Unreported line	-	+123,467.401 (32)
Unreported line	-	+204,269.162 (33)

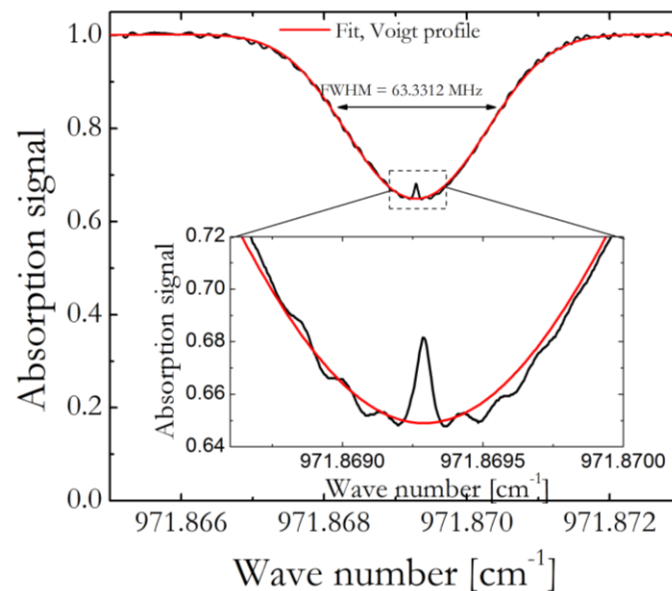
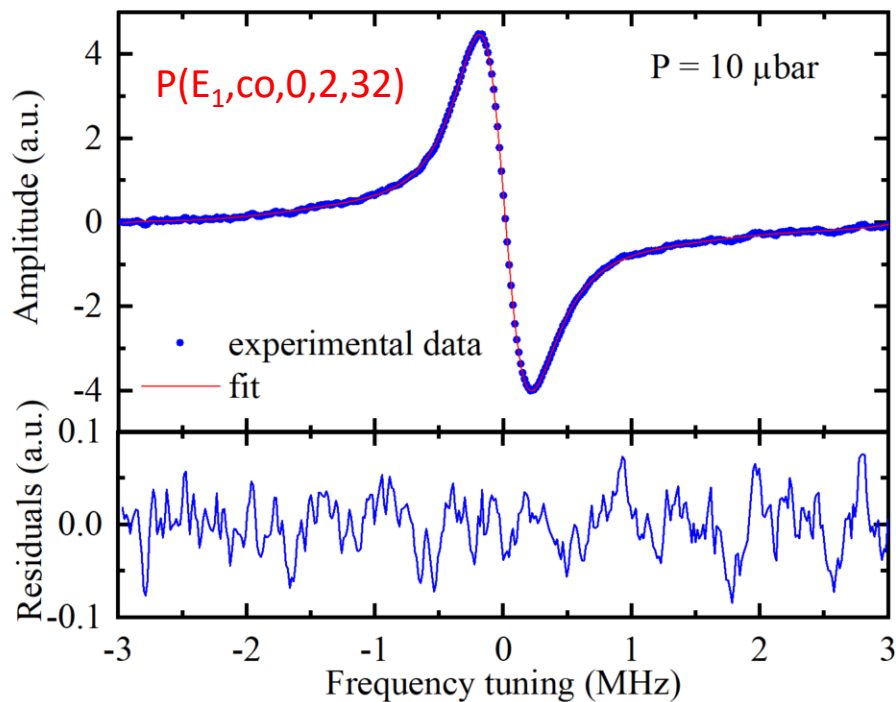
# High-resolution spectroscopy of methanol

saturated absorption spectroscopy in a multi-pass cell



# High-resolution spectroscopy of methanol

P(32, 2) E<sub>1</sub> line, C-O stretch



- FM @ 20 kHz, deviation 50 kHz
- 1st harmonic detection
- 100 ms lock-in amplifier time constant

# Summary / Perspectives

- Precise and tuneable frequency control of a mid-IR QCL referenced to a comb
  - stability and accuracy transfer from 1.54  $\mu\text{m}$  to 10  $\mu\text{m}$
  - direct link to primary frequency standards
  - record stabilities/accuracies:
    - 0.05 Hz ( $2 \times 10^{-15}$ ) stability @ 1 s
    - 0.1 Hz line width
    - 0.3 Hz ( $10^{-14}$ ) accuracy, potentially 0.01 Hz ( $3 \times 10^{-16}$ )
  - anywhere in 5-20  $\mu\text{m}$  region potentially,  $\sim 1$  GHz continuous tuning
- Saturated absorption spectroscopy of OsO<sub>4</sub>/methanol
  - $\sim 10$  Hz/ $\sim 1$  kHz uncertainty on the absolute frequency
  - new lines and patterns unreported so far
- Precision spectroscopic measurement with polyatomic molecules
  - tests of fundamental physics → measuring parity violation in chiral molecules talk by A. Cournol on Friday (FD04)
  - metrology → Doppler broadening thermometry talk on Friday (FD03)
  - atmospheric physics, astrophysics, collisions,...



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