

# Mid-infrared frequency-agile dual-comb spectroscopy

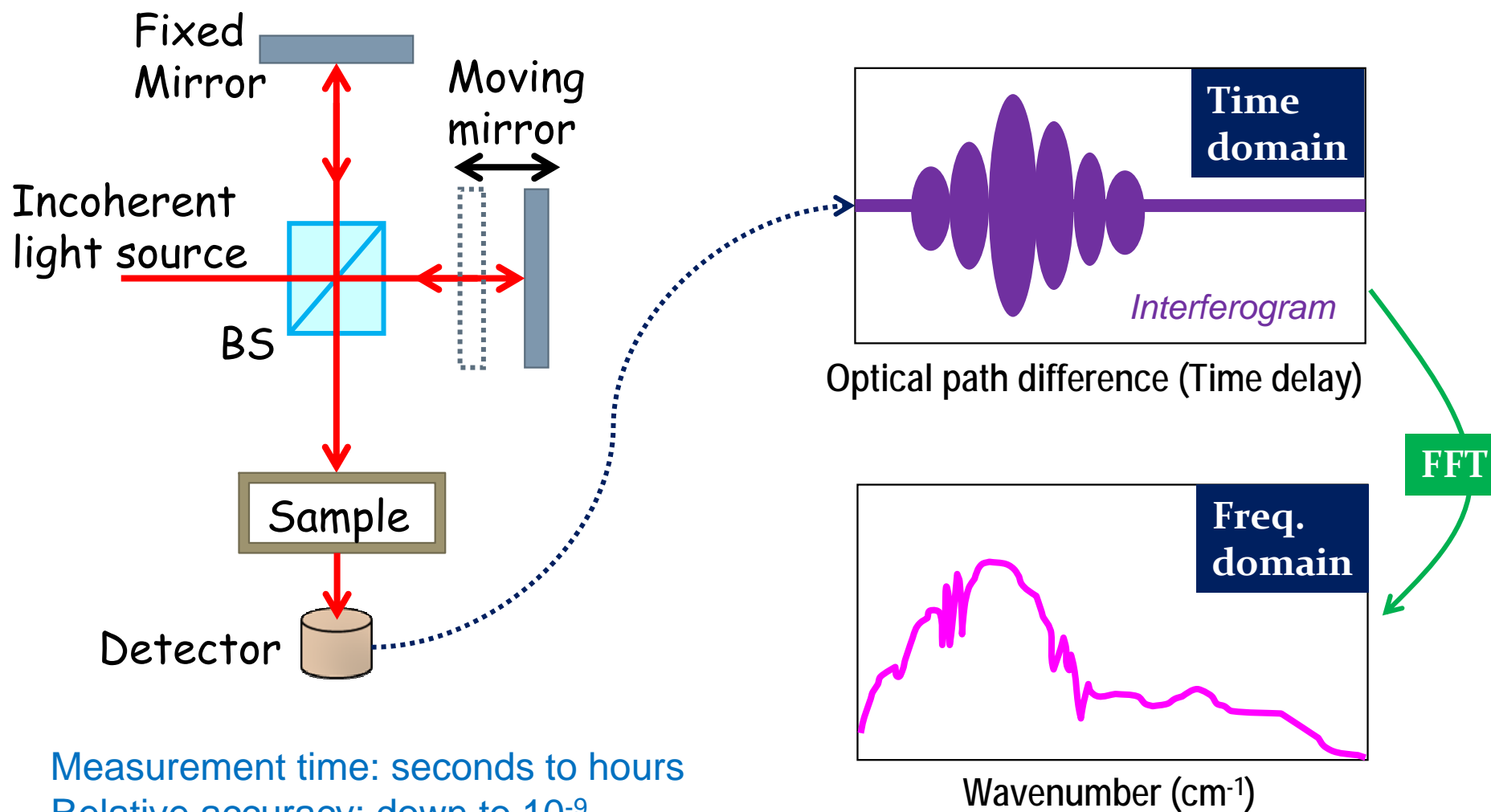
---

Pei-Ling Luo<sup>1,2</sup>, Ming Yan<sup>1,2</sup>, Kana Iwakuni<sup>1,2</sup>, Guy Millot<sup>3</sup>,  
Theodor W. Hänsch<sup>1,2</sup>, Nathalie Picqué<sup>1,2</sup>

1. Max-Planck-Institut für Quantenoptik, Germany
2. Ludwig-Maximilians-Universität München, Germany
3. Laboratoire ICB, CNRS/Université de Bourgogne,  
DIJON, France

# Most widely used spectrometer in mid-infrared

## Fourier transform spectrometer (FTS)

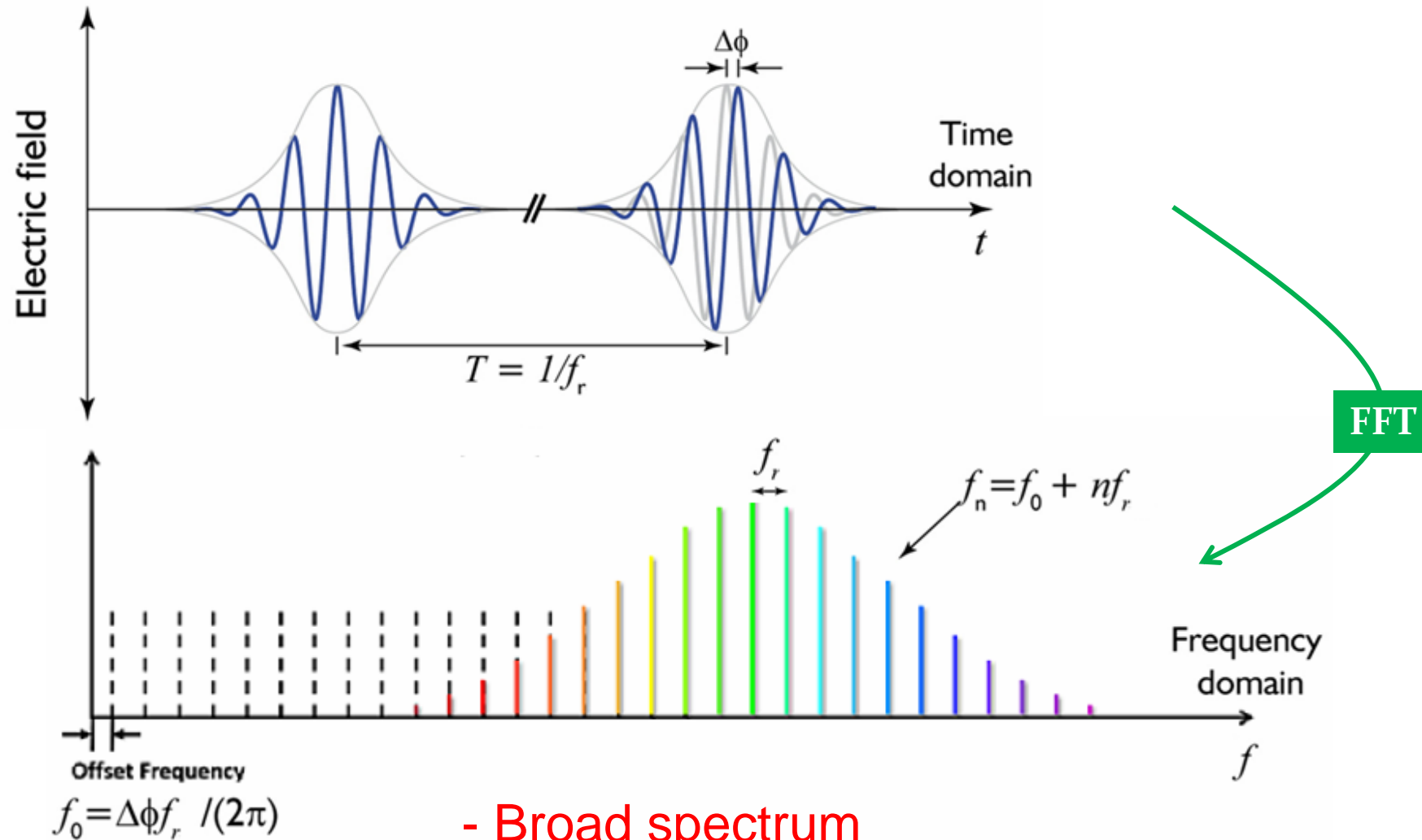


Measurement time: seconds to hours

Relative accuracy: down to  $10^{-9}$

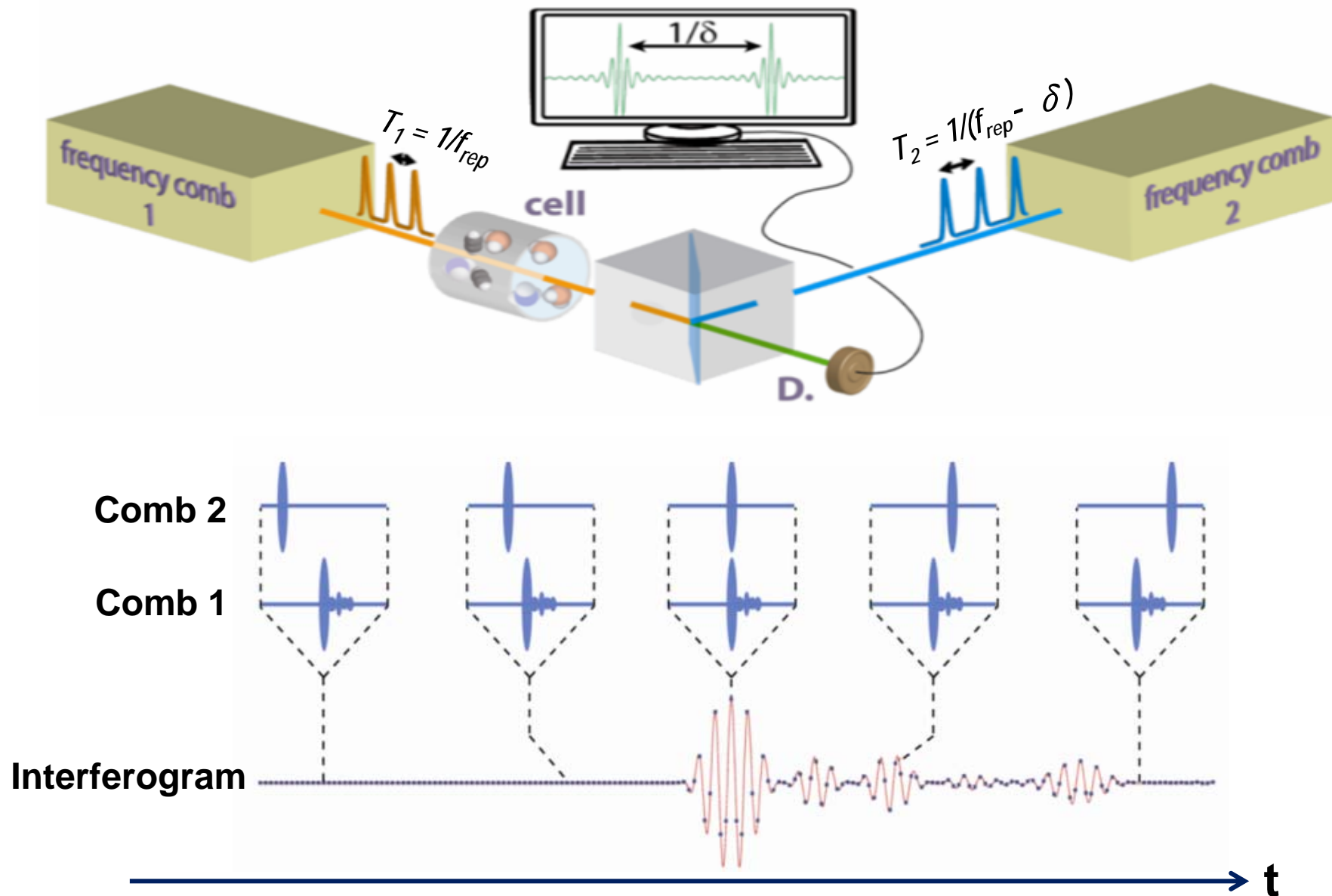
Resolution: down to  $0.001 \text{ cm}^{-1}$

# Optical Frequency combs

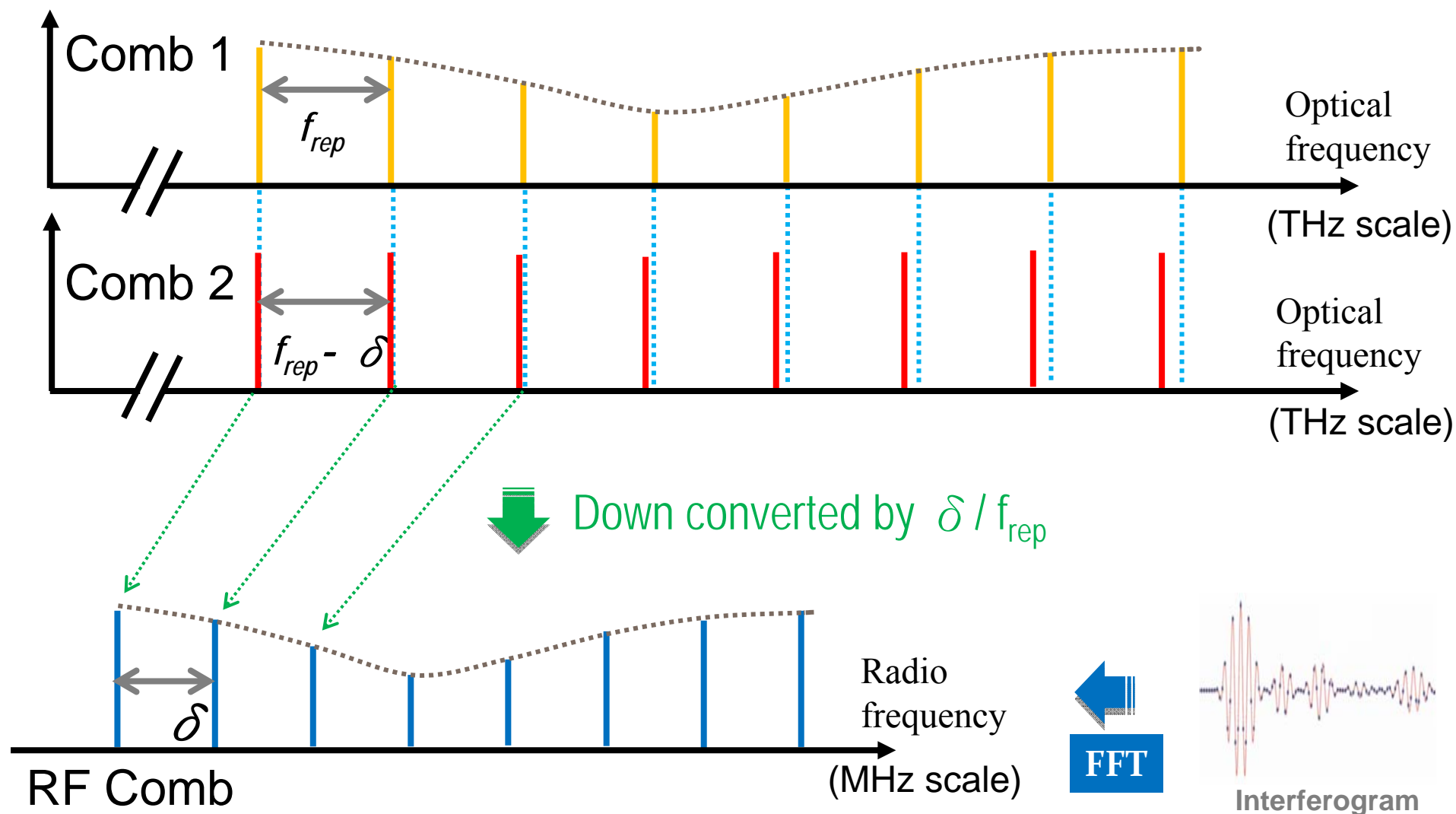


- Broad spectrum
- Many narrow comb lines

# Principle of dual-comb spectroscopy in time domain



# Principle of dual-comb spectroscopy in frequency domain



# Dual-comb spectroscopy

## New approach to MIR dual-comb spectroscopy

Without mode-locked lasers and phase-lock electronics

NIR Frequency-agile  
laser combs

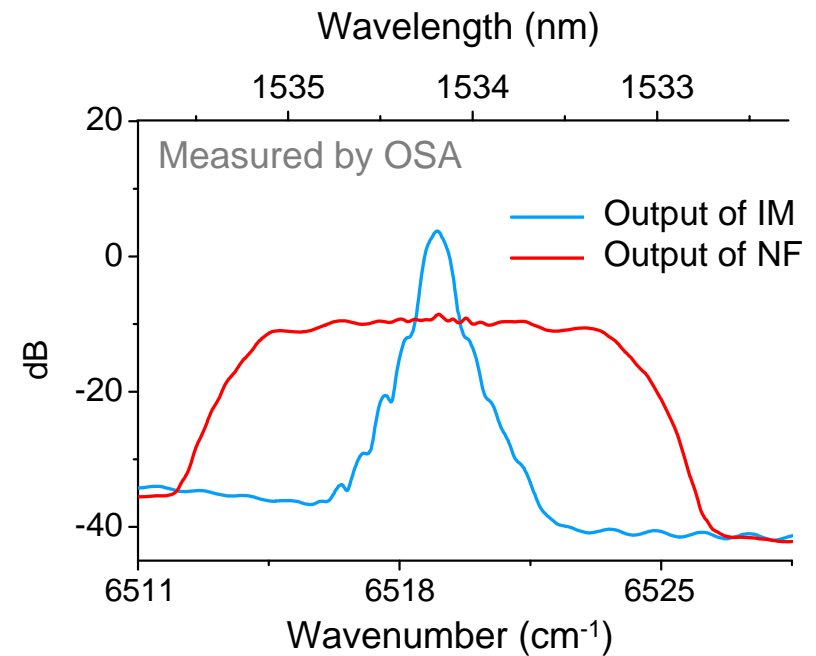
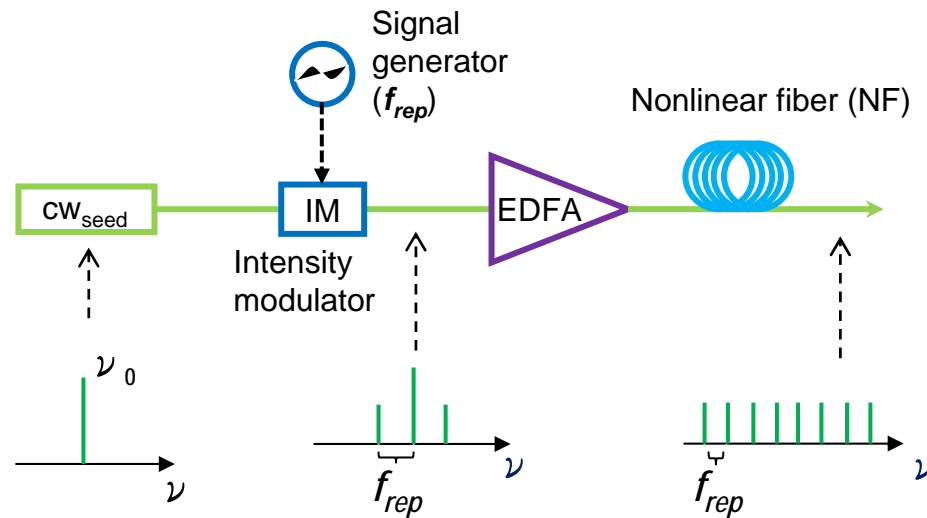
+

Difference frequency  
generation to MIR

+

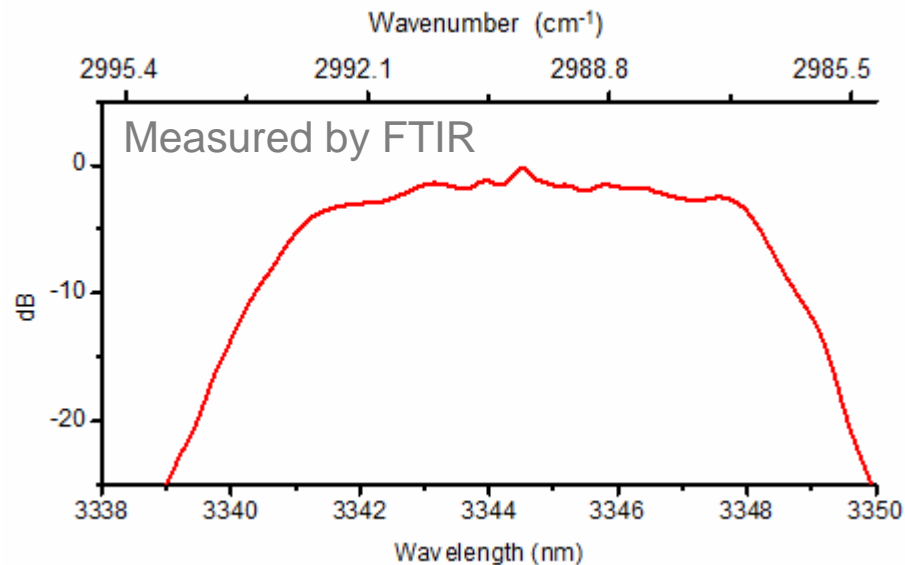
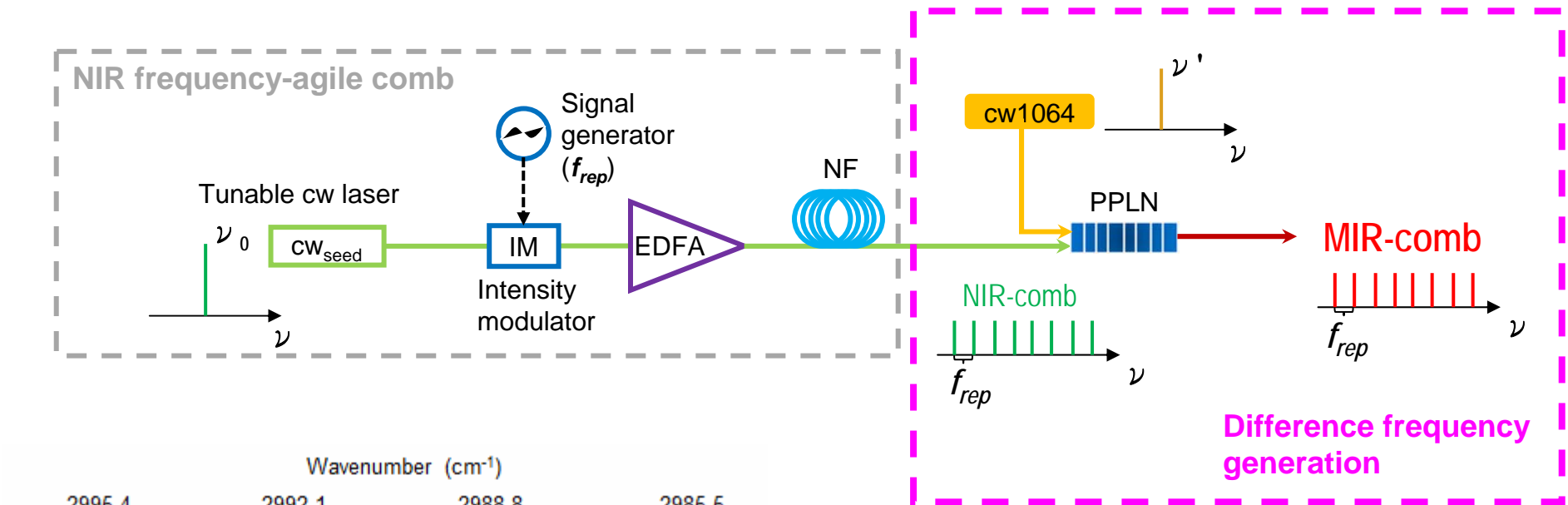
Multi-heterodyne  
detection

# Frequency-agile laser combs in NIR



- ✓ Simplicity without mode-locked lasers
- ✓ Flat-top spectrum with up to 2000 comb lines (within 3 dB)
- ✓ Widely & simply tunable comb line spacing (100 MHz ~ 1000 MHz)  
( $3.3 \times 10^{-3} \text{ cm}^{-1} \sim 3.3 \times 10^{-2} \text{ cm}^{-1}$ )

# Mid-infrared Frequency-agile laser combs

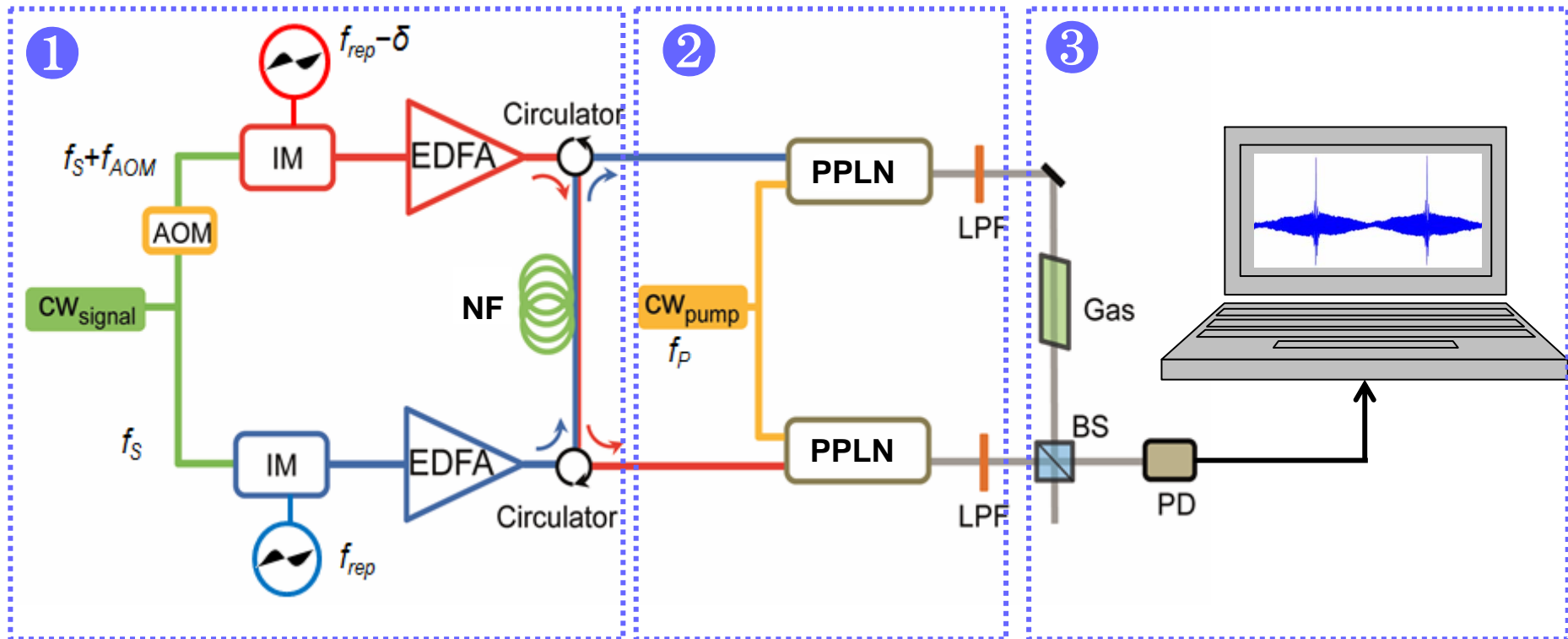


Optical resolution: 6 GHz ( $0.2\text{ cm}^{-1}$ )

- ✓ Average power:  $> 500\text{ }\mu\text{W}$
- ✓ Spectral bandwidth:  $7\sim 10\text{ cm}^{-1}$
- ✓ Wavelength tunable:  $2800\sim 3200\text{ cm}^{-1}$   
( $3100\sim 3500\text{ nm}$ )

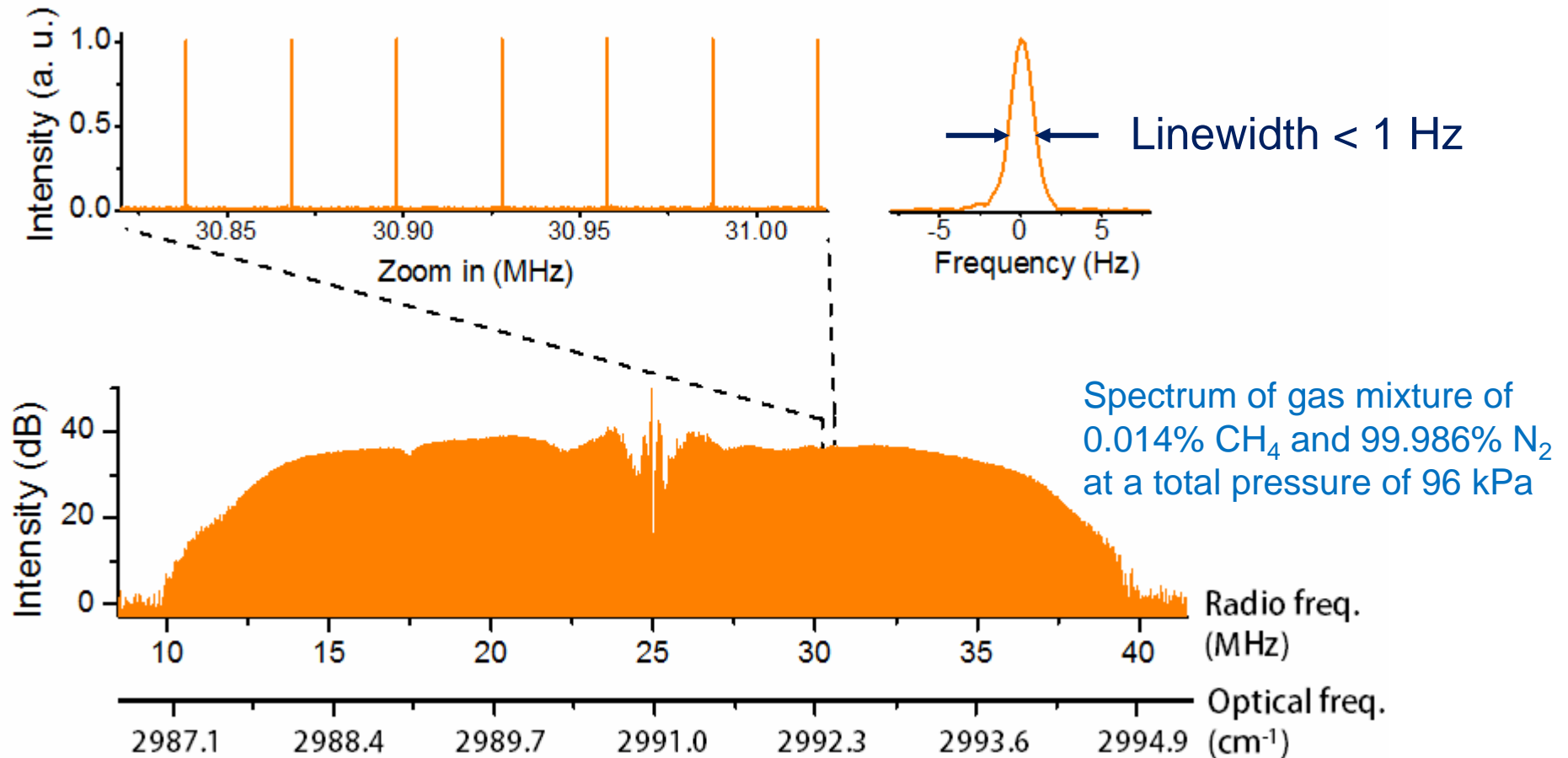


# MIR Frequency-agile dual-comb spectroscopy



1. Generation of two NIR frequency combs with flat-top spectral profiles
2. MIR frequency comb generation by the difference frequency generation
3. Dual-comb Fourier transform spectroscopy

# MIR Frequency-agile dual-comb spectroscopy



Measurement time: 1.1 sec; Optical resolution: 230 MHz ( $\sim 7.7 \times 10^{-3} \text{ cm}^{-1}$ )

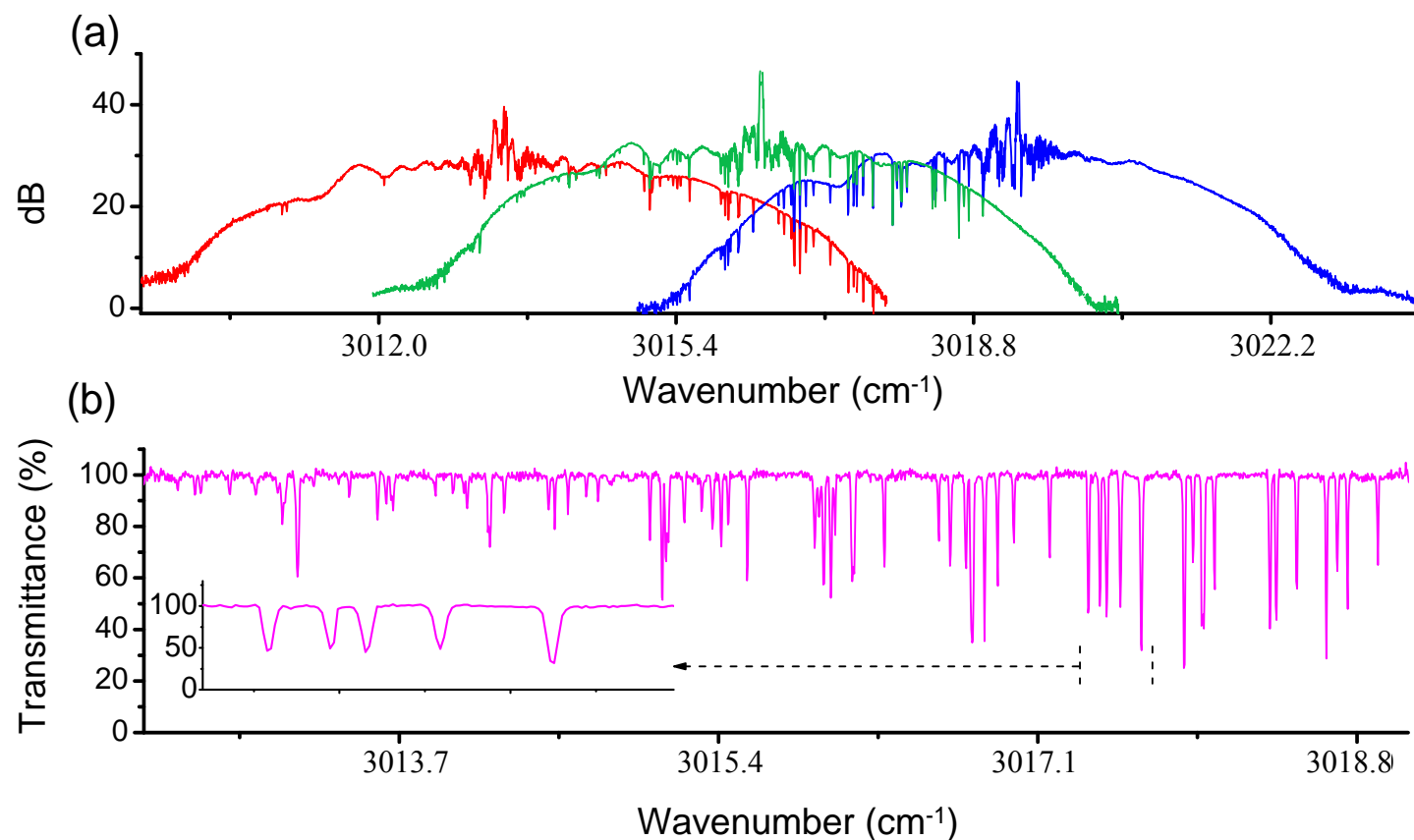
**Rules for RF domain  $\rightarrow$  Optical frequency domain**

Center peak  $\rightarrow f(\text{CW}_{\text{pump}}) - f(\text{CW}_{\text{signal}})$

Comb line spacing in RF domain  $\times f_{\text{rep}} / \delta \rightarrow$  Optical frequency domain

# Mid-infrared dual-comb spectra with frequency agility

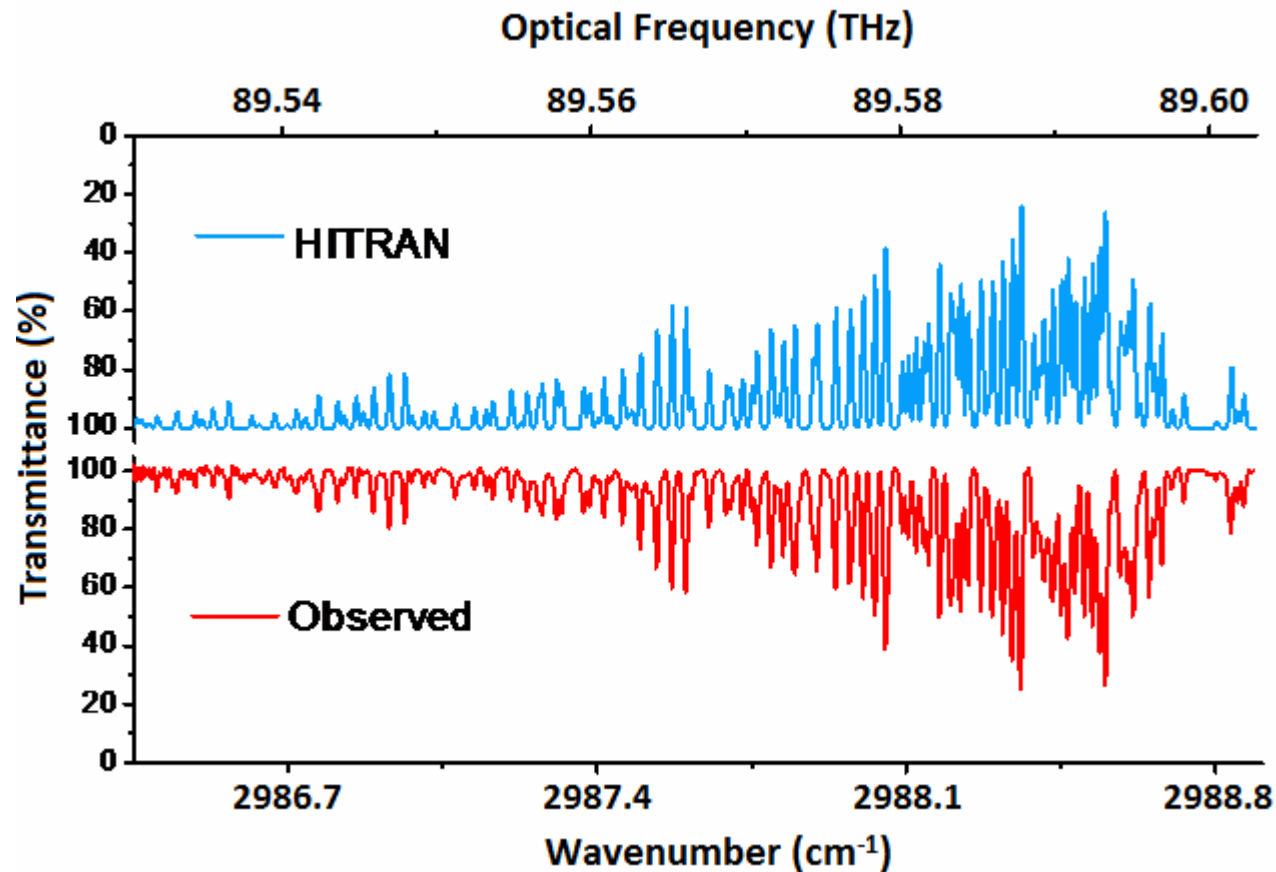
## Q-branch of methane gas ( $\nu_3$ band)



- Measurement time for each spectrum: 72 ms ( $728 \mu\text{s} \times 100$ )
- Resolution: 115 MHz ( $\sim 5 \times 10^{-3} \text{ cm}^{-1}$ )

# Mid-infrared dual-comb spectrum with Doppler-limited resolution

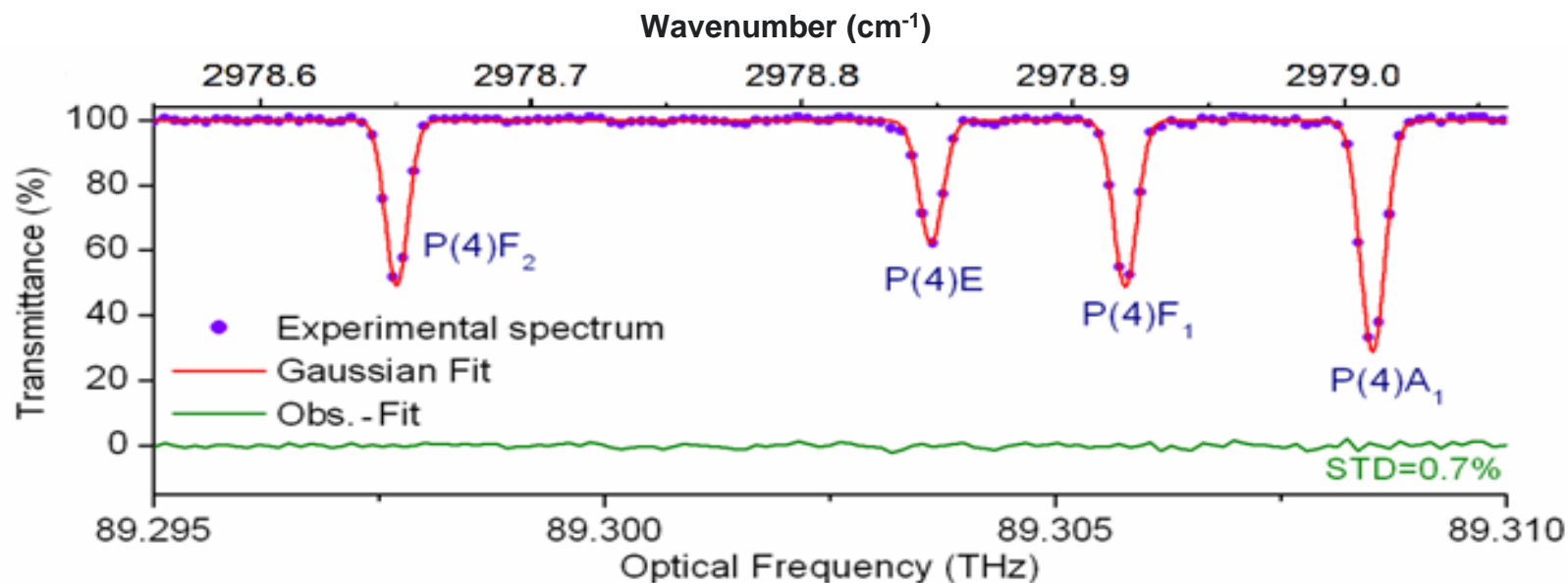
Q-branch of ethylene gas ( $\nu_{11}$  band)



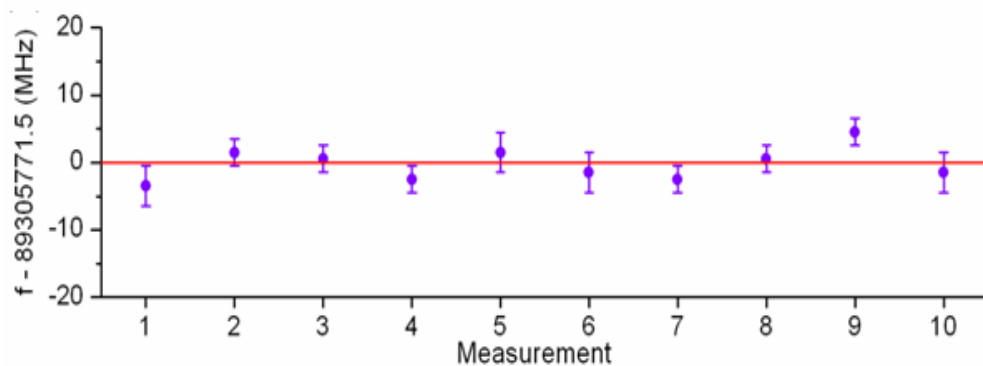
- Total measurement time: 72 ms ( $728 \mu\text{s} \times 100$ )
- Resolution: 100 MHz ( $\sim 3.3 \times 10^{-3} \text{ cm}^{-1}$ )

# Precision measurements of line position and intensity

The  $\nu_3$  band P(4) lines of  $\text{CH}_4$



- Measurement time: 72 ms
- Resolution: 115 MHz ( $\sim 5 \times 10^{-3} \text{ cm}^{-1}$ )



10 measurements of the  $P(4)F_1$  line position

✓ Line position measurements for Doppler-limited spectra

→ Relative accuracy of  $10^{-8}$   
(a few MHz uncertainty)

✓ Line intensity measurements

→ 1~3% uncertainty

# Precision measurements of line position and intensity

## Line positions

Line	This work (MHz)	Ref. 1 (MHz)	This work – Ref. 1 (MHz)
P(4) F <sub>2</sub>	89297694.9(1.2)	89297695.2635(21)	-0.4
P(4) E	89303617.9(1.3)	89303620.0492(25)	-2.1
P(4) F <sub>1</sub>	89305771.5 (1.1)	89305771.6093(21)	-0.1
P(4) A <sub>1</sub>	89308513.3(1.1)	89308512.2568(20)	1.0

Ref. 1: Absolute frequency list of the  $\nu_3$ -band transitions of methane at a relative uncertainty level of  $10^{-11}$ , Opt. Express 19, 23878-23888 (2011)

## Line intensities

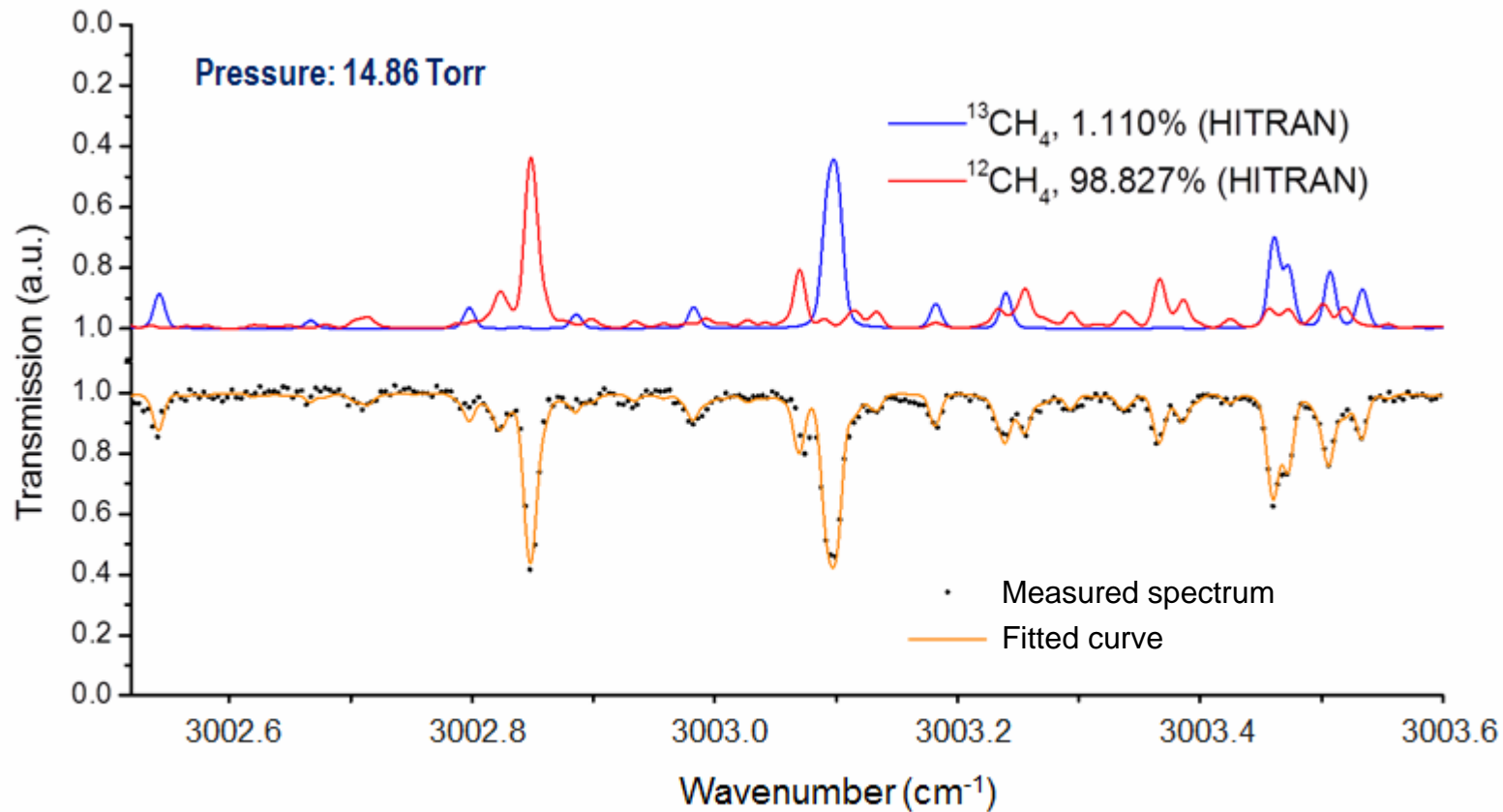
Line	This work* (cm <sup>-1</sup> /mol*cm <sup>-2</sup> )	Ref. 2 (cm <sup>-1</sup> /mol*cm <sup>-2</sup> )	Difference (%)
P(4) F <sub>2</sub>	7.134(133)×10 <sup>-20</sup>	7.310(147)×10 <sup>-20</sup>	-2.41
P(4) E	4.796(132)×10 <sup>-20</sup>	4.887(98)×10 <sup>-20</sup>	-1.86
P(4) F <sub>1</sub>	7.245(132)×10 <sup>-20</sup>	7.339(147)×10 <sup>-20</sup>	-1.28
P(4) A <sub>1</sub>	1.2060(196)×10 <sup>-19</sup>	1.215(25)×10 <sup>-19</sup>	-1.71

\* The intensities here have been corrected for the purity of methane (99.95%) and the isotopic abundance (98.827% for <sup>12</sup>CH<sub>4</sub>). The uncertainty includes 1% pressure error, 1% cell length error, and 1 K temperature error.

Ref. 2: N<sub>2</sub> and Ar broadening and line mixing in the *P* and *R* branches of the  $\nu_3$  band of CH<sub>4</sub>, J. Quant. Spectrosc. Radiat. Transf. 57, 157–176 (1997)

# Accurate Concentration measurements of isotopes ( $^{12}\text{C}/^{13}\text{C}$ ) in methane

☑ Concentration measurements → ~2% uncertainty



- Total measurement time: 72 ms ( $728 \mu\text{s} \times 100$ )
- Resolution: 115 MHz ( $\sim 5 \times 10^{-3} \text{ cm}^{-1}$ )

## Summary

- **Mid-IR frequency-agile comb**
  - ✓ Without mode-locked lasers & phase-lock electronics
  - ✓ Flat-top spectral profile with 1000 comb lines
  - ✓ Widely tunable comb line-spacing & center wavelength
- **Mid-IR frequency-agile dual-comb spectroscopy**
  - ✓ Dual-comb Fourier transform spectrometer
    - Broadband measurement available
    - Resolved comb line without instrumental lineshape
  - ✓ Precision measurements of Doppler-limited dual-comb spectra in tens of ms measurement time
    - Line position measurement → relative accuracy of  $10^{-8}$
    - Line intensity measurement → 1~3% uncertainty
  - ✓ Accurate concentration measurements of ( $^{12}\text{C}/^{13}\text{C}$ ) in methane

## Outlook

- ✓ Turnkey system for environment tracing
- ✓ Real-time gas sensing (gas concentration & composition)